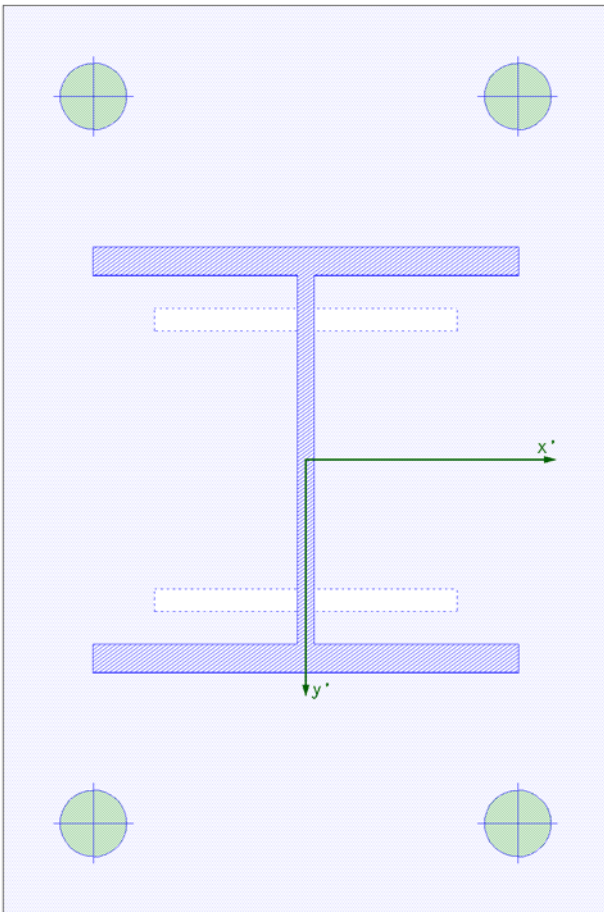


## steel column base with base plate on isolated foundation

steel code verifications acc. to DIN EN 1993-1:2010-12 with NA-Deutschland  
reinf. concr. design acc. to DIN EN 1992-1-1:2011-01 with NA-Deutschland(DIN EN 1992-1-1/NA:2013-04)  
external stability acc. to DIN EN 1997-1:2014-03 with NA-Deutschland  
additional rules acc. to DIN 1054:2021-04 , DIN 4017:2006-03 and DIN 4019:2015-05

top view base plate  
scale 1:5



### column cross section

standardized profile: HE280B, of quality S275 N/NL

### base plate

$b_x = 400 \text{ mm}$   $b_y = 600 \text{ mm}$   $t = 60 \text{ mm}$ , of quality S275 N/NL

### mortar joint

$t_F = 20 \text{ mm}$

### shear connector

standardized profile: HE200B, of quality S235

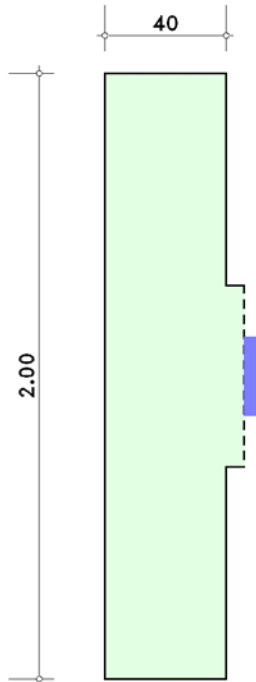
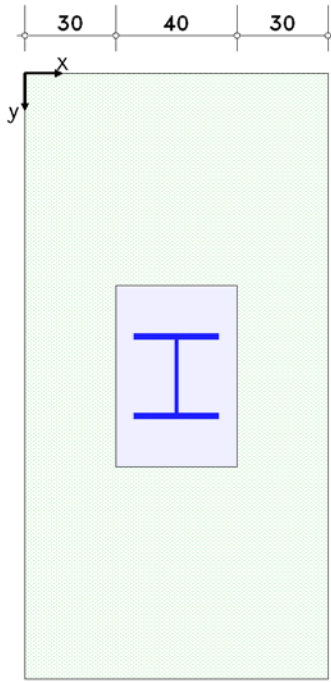
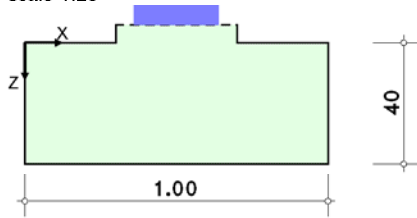
### anchors

4 anchors, FK 5.8, M24, without shaft

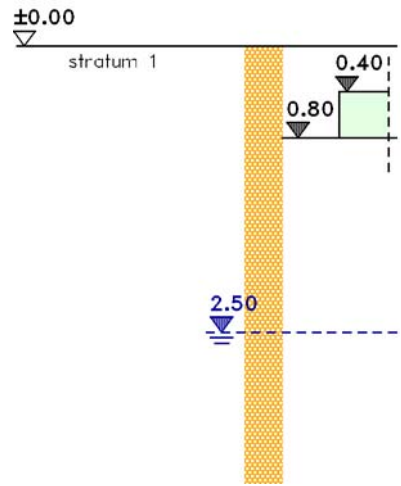
with a length of 450 mm

edge distances  $a_x/a_y = 60/60 \text{ mm}$

elevation, top view isolated foundation  
scale 1:25



soil profile



concrete strength class C30/37  
steel class B500A

## 1. soil situation

the anchoring depth of the foundation is  $t = 0.80$  m.  
the ground water level (below top edge soil) is at  $t_w = 2.50$  m.

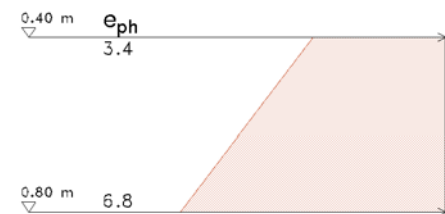
### 1.1. designation and characteristic values of soil strata

stratum	d m	z m	$\gamma$ kN/m <sup>3</sup>	$\gamma'$ kN/m <sup>3</sup>	$\phi$ °	$c_k$ kN/m <sup>2</sup>	$E_m$ MN/m <sup>2</sup>	$\delta_p$ °
stratum 1	99.00	0.00	20.00	11.00	35.0	---	80.00	auto

z - levelan top edge der stratum  $\gamma$  - unit weight  $\gamma'$  - unit weight of submerged soil  $\phi$  - friction angle  
 $c_k$  - char. cohesion of the dained soil  $E_m$  - mean compression modulus  $\delta_p$  - angle of wall friction on the passive side

### 1.2. char. passive earth pressure

Als passive earth pressure wird der earth pressure at rest angesetzt.



$\Sigma(\gamma \cdot h)$  Summe soilgewicht in der betrachteten Tiefe  
 $\Sigma(\gamma \cdot h)_{cal}$  Summe soilgewicht in der betrachteten Tiefe zuzüglich Böschungseinfluß  
 $K_{0gh}$  coeff. of earth pressure acc. to [1] clause 6.2.1, Gl.(7) (formulation acc. to Müller-Breslau)  
 $e_{0h}$  horiz. Erddruckordinate

z m	$\Sigma(\gamma \cdot h)$ kN/m <sup>2</sup>	$\Sigma(\gamma \cdot h)_{cal}$ kN/m <sup>2</sup>	$K_{0gh}$ -	$e_{0h}$ kN/m <sup>2</sup>
0.40	8.00	12.00	0.426	3.41
0.80	16.00	16.00	0.426	6.82





the resultant maximum passive earth pressure is  $E_{0hg} = 2.05$  kN/m, at  $z_s = 0.62$  m.

## 2. loading

### 2.1. Structure of action effects

On the left-hand side, the action effects and load cases are shown in a tree structure. The right-hand side shows their characteristics of the superposition.

used symbols:  action  load case

 1: permanent loads	<b>permanent loads</b>
└  1: dead load (1)	additive
 2: live loads (2)	<b>variable live loads in assembly and salesrooms</b>
└  2: live loads (2/1)	additive

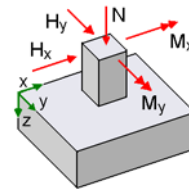
### 2.2. Design calculation situation of load cases for external stability

loadc.	notation	BS-P	BS-T
1	dead load (1)	x	
2	live loads (2/1)	x	

### 2.3. Characteristic column load

point of application in column centroid auf top edge foundation slab

loadc.	N <sub>st</sub> kN	H <sub>x,St</sub> kN	H <sub>y,St</sub> kN	M <sub>x,St</sub> kNm	M <sub>y,St</sub> kNm
1	200.00	0.00	30.00	50.00	0.00
2	100.00	0.00	50.00	75.00	0.00



### 2.4. dead load

Das Gewicht der foundation slab wird with  $\gamma_E = 25.00 \text{ kN/m}^3$  berücksichtigt.

the height of the earth load is  $h_A = 0.40 \text{ m}$ .

the mean unit weight of the earth load is  $\gamma_A = 20.00 \text{ kN/m}^3$ .

the resultant of dead load in the floor joint is  $N_{0,dead1,k} = 34.08 \text{ kN}$ .

Das dead load wird im load case 1 with berücksichtigt.

## 3. Verification of steel column base

### 3.1. partial safety factors for material

design situat.	$\gamma_{M0}$	$\gamma_{M2}$	$\gamma_c$
permanent	1.00	1.25	1.50

### 3.2. design values of steel verifications

#### 3.2.1. factorization of load case combinations

LK	design situat.	factorization
1	permanent and transient	Lf1
2	permanent and transient	1.35·Lf1
3	permanent and transient	Lf1+1.5·Lf2
4	permanent and transient	1.35·Lf1+1.5·Lf2

#### 3.2.2. column load

increasing factor for flex. mom.:  $\Delta M_{St,TH,II,0} = M_{St} \cdot 20\%$   
(for the consideration of increase of moments from non-linear effects)

LK	N <sub>St,d</sub> kN	H <sub>x,St,d</sub> kN	H <sub>y,St,d</sub> kN	M <sub>x,St,d</sub> kNm	M <sub>y,St,d</sub> kNm
1	200.00	0.00	30.00	60.00	0.00
2	270.00	0.00	40.50	81.00	0.00
3	350.00	0.00	105.00	195.00	0.00
4	420.00	0.00	115.50	216.00	0.00

### 3.3. weld between column shaft and base plate

design with direction oriented method acc. to clause 4.5.3.2

$$\sigma_{V,w,Ed} = (\sigma_{\perp}^2 + 3 \cdot \tau_{\perp}^2 + 3 \cdot \tau_{\parallel}^2)^{0.5}$$

$$f_{1,w,Rd} = f_u / (\beta_w \cdot \gamma_{M2})$$

$$f_{2,w,Rd} = 0.9 f_u / \gamma_{M2}$$

$$U = \max\{ \sigma_{V,w,Ed} / f_{1,w,Rd}, \sigma_{\perp} / f_{2,w,Rd} \}$$

connection designed with a full-size double fillet weld.

axial force transfer of 30 % by the weld.

minimum value of the weld thickness  $a_{min} = 8 \text{ mm}$

LK	$a_{w,F1}$ mm	$a_{w,S}$ mm	$\sigma_{\perp}$ kN/cm <sup>2</sup>	$\tau_{\perp}$ kN/cm <sup>2</sup>	$\tau_{\parallel}$ kN/cm <sup>2</sup>	$\sigma_{V,w,Ed}$ kN/cm <sup>2</sup>	$f_{1,w,Rd}$ kN/cm <sup>2</sup>	$f_{2,w,Rd}$ kN/cm <sup>2</sup>	Maßgeb.	U
1	8	8	-4.32	-4.32	0.00	8.65	36.71	28.08	f lange	0.24
2	8	8	-5.84	-5.84	0.00	11.68	36.71	28.08	f lange	0.32
3	8	8	-13.48	-13.48	0.00	26.97	36.71	28.08	f lange	0.73
4	8	8	-15.00	-15.00	0.00	29.99	36.71	28.08	f lange	<b>0.82</b>

maximum weld thickness flange  $a_{w,F1,max} = 8$  mm

maximum weld thickness of the web  $a_{w,S,max} = 8$  mm

maximum utilization  $U = 0.82 < 1.00$

$a_{w,F1}$  - flange weld thickness    $a_{w,S}$  - web weld thickness    $a_w$  - weld thickness    $\sigma_{\perp}$  - normal stresses perpendicular to weld  
 $\tau_{\perp}$  - shear stresses perpendicular to weld    $\tau_{\parallel}$  - shear stresses parallel to weld   U - utilization

### 3.4. FE-calculation

The calculation of pressures under the base plate and of the base plate decisive internal forces and moments is done by a FEM-calculation using constrained modulus method. The initial bedding of the plate results from the concrete modulus of elasticity under the base plate. Tension springs are eliminated in elastic bedded areas. Anchors are considered as point springs only acting in case of tension.

The plate is divided into 22 elements in X-direction and 35 elements in Y-direction.

The concrete compression is limited to the allowable partial area pressure with  $\lim \sigma_{c,d} = f_{Rd,u}$ .

The equivalent spring for the anchors is applied with  $c = E \cdot A / l = 1647.33$  kN/cm.

#### 3.4.1. stresses in base plate (elast.-plast.)

##### internal forces and moments

LK	$x_{Fp}$ cm	$y_{Fp}$ cm	$m_{xx}$ kNcm/cm	$m_{yy}$ kNcm/cm	$m_{xy}$ kNcm/cm	$v_x$ kN/cm	$v_y$ kN/cm
1	19.1	14.6	12.10	28.26	0.78	0.61	-1.94
2	19.1	14.6	16.39	38.28	1.06	0.82	-2.63
3	20.9	14.6	46.78	111.69	-2.82	-2.25	-8.35
4	19.1	14.6	51.63	122.97	3.14	2.50	-9.11

##### stresses and utilizations

$$\sigma_{Pl,V} = (\sigma_x^2 + \sigma_y^2 - \sigma_x \sigma_y + 3(\tau_{xy}^2 + \tau_{xz}^2 + \tau_{yz}^2))^{0.5}$$

$$\sigma_{Rd} = f_y / \gamma_{M0}$$

$$U = \sigma_{Pl,V} / \sigma_{Rd}$$

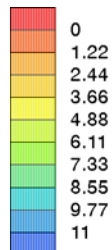
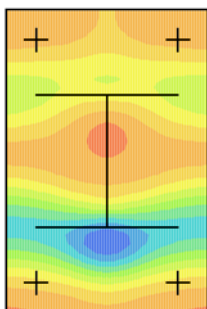
LK	$x_{Fp}$ cm	$y_{Fp}$ cm	$\sigma_{Pl,V}$ kN/cm <sup>2</sup>	$\sigma_{Rd}$ kN/cm <sup>2</sup>	U
1	19.1	14.6	2.80	25.50	0.11
2	19.1	14.6	3.79	25.50	0.15
3	20.9	14.6	11.09	25.50	0.44
4	19.1	14.6	12.21	25.50	<b>0.48</b>

maximum utilization  $U = 0.48 < 1.00$

$x_{Fp}/y_{Fp}$  - coordinates on the base plate    $m_{xx}/m_{yy}$  - flex. mom.    $m_{xy}$  - torsional mom.    $v_x/v_y$  - shear force  
 $\sigma_{Pl,V}$  - plastic equivalent stress    $\sigma_{Rd}$  - limit normal stress   U - utilization

#### stress distribution - $\sigma_{Pl,V}$ [kN/cm<sup>2</sup>]

LK 4 (max  $\sigma_{Pl,V}$ )



#### 3.4.2. concrete compression under base plate

$$f_{cd} = \alpha_{cc} \cdot f_{ck} / \gamma_c$$

$$U_{fjd} = \sigma_{c,m} / f_{jd}$$

$$U_{A,compression} = \text{axis} (A_{\sigma c > f_{jd}} / A_{compression}) / \text{perm} (A_{\sigma c > f_{jd}} / A_{compression})$$

design value der concrete- resp. Mörtelfestigkeit unter bearing stress:  $f_{jd} = 1.0 \cdot f_{cd}$

verification nur at surface of pressuren größer als 5% der slab nfläche ( $A_{compression} > 120.0$  cm<sup>2</sup>)

control of heavily loaded compression areas:

the allowable relation between the area with concrete compressions greater than the design value

( $A_{\sigma c > f_{jd}}$ ) and the total compression area ( $A_{compression}$ ) comes to:  $\text{perm} (A_{\sigma c > f_{jd}} / A_{compression}) = 30\%$

LK	lim $\sigma_{c,d}$ kN/cm <sup>2</sup>	A <sub>compression</sub> cm <sup>2</sup>	F <sub>compression</sub> kN	F <sub>compression</sub> cm <sup>2</sup>	A <sub><math>\sigma_c &gt; f_{jd}</math></sub> kN/cm <sup>2</sup>	$\sigma_{c,max}$ kN/cm <sup>2</sup>	$\sigma_{c,m}$ kN/cm <sup>2</sup>	-	f <sub>jd</sub>	U <sub>fjd</sub>	A <sub><math>\sigma_c &gt; f_{jd}</math></sub> / A <sub>compression</sub> %
1	5.10	941.3	251.22	-	0.75	0.267	1.70	0.16		0.00	
2	5.10	941.3	339.49	-	1.01	0.361	1.70	0.21		0.00	
3	5.10	822.9	619.69	6.2	1.75	0.753	1.70	0.44		0.76	
4	5.10	822.9	710.07	31.2	2.01	0.863	1.70	<b>0.51</b>		<b>3.79</b>	

maximum utilization  $U_{fjd} = 0.51 < 1.00$

maximum share of the compression area with  $\sigma_c > f_{jd}$ :  $A_{\sigma_c > f_{jd}}/A_{compression} = 3.79 < 30.00\%$

associated utilization  $U_{A,compression} = 0.13 < 1.00$

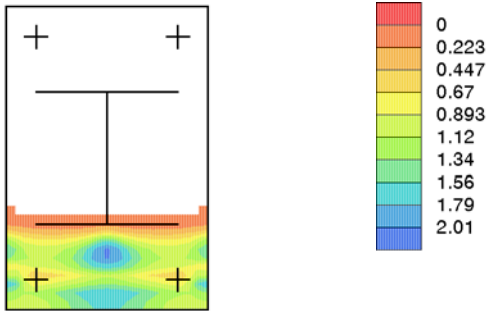
A<sub>compression</sub> - area with concrete compressions F<sub>compression</sub> - Res. compressionkraft auf den concrete  $\sigma_{c,max}$  - maximale concrete compression

$\sigma_{c,m}$  - mean concrete compression U<sub>fjd</sub> - utilization withtl. bearing stress

U<sub>A,compression</sub> - utilization of the allowable compr. area with  $\sigma_c > f_{cd}$   $\sigma_c > f_{jd}$

### pressure distribution [kN/cm<sup>2</sup>]

LK 4 (max  $\sigma_{c,m}$ )



### 3.4.3. anchor tensile forces

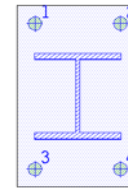
$$F_{t,Rd} = k_2 \cdot f_{ub} \cdot A_s / \gamma_{M2}$$

$$U = F_{t,Ed,max} / F_{t,Rd}$$

stress area of M24:  $A_s = 3.53 \text{ cm}^2$

No countersunk bolts used:  $k_2 = 0.90$

numeration



LK	F <sub>t,Ed,1</sub> kN	F <sub>t,Ed,2</sub> kN	F <sub>t,Ed,3</sub> kN	F <sub>t,Ed,4</sub> kN	F <sub>t,Rd</sub> kN	U <sub>max</sub> -
1	25.61	25.61	---	---	127.08	0.20
2	34.75	34.75	---	---	127.08	0.27
3	134.84	134.84	---	---	127.08	1.06
4	145.03	145.03	---	---	127.08	<b>1.14</b>

maximum utilization  $U = 1.14 > 1.00 \Rightarrow$  allowable tension force exceeded

!!

f<sub>ub</sub> - tensile strength of bolt material F<sub>t,Ed,i</sub> - anchor tension force F<sub>t,Rd</sub> - design tension resistance of anchors

U<sub>max</sub> - max. utilization

### 3.5. shear connector for transfer of horizontal force into the foundation

total length  $l = 22.0 \text{ cm}$

length in concrete  $l_c = 20.0 \text{ cm}$

#### 3.5.1. concrete compression

$$\sigma_c = V_{Ed} / (l_c \cdot b)$$

$$U = \sigma_{c,max} / f_{cd}$$

LK	V <sub>Ed,flange</sub> kN	V <sub>Ed,web</sub> kN	$\sigma_{c,flange}$ N/mm <sup>2</sup>	f <sub>cd</sub> N/mm <sup>2</sup>	U
1	30.00	0.00	2.50	17.00	0.15
2	40.50	0.00	2.89	17.00	0.17
3	105.00	0.00	2.92	17.00	<b>0.17</b>
4	115.50	0.00	2.89	17.00	0.17

maximum utilization  $U = 0.17 < 1.00$

$\sigma_{c,flange}$  - concrete compression by flange U - utilization

### 3.5.2. stresses in connection of base plate

$$\sigma_{v,Ed} = (\sigma_{Ed}^2 + 3 \cdot \tau_{Ed}^2)^{0.5}$$

$$\sigma_{Rd} = f_y / \gamma_{M0}$$

$$U = \sigma_{v,Ed} / \sigma_{Rd}$$

LK	$M_{x,Ed}$ kNcm	$M_{y,Ed}$ kNcm	$\sigma_{Ed}$ kN/cm <sup>2</sup>	$\tau_{Ed}$ kN/cm <sup>2</sup>	$\sigma_{v,Ed}$ kN/cm <sup>2</sup>	$\sigma_{Rd}$ kN/cm <sup>2</sup>	U
1	150.00	0.00	0.26	1.81	3.14	23.50	0.13
2	222.75	0.00	0.39	2.45	4.24	23.50	0.18
3	1155.00	0.00	2.03	6.35	10.99	23.50	0.47
4	1386.00	0.00	2.43	6.98	12.09	23.50	0.51

maximum utilization  $U = 0.51 < 1.00$

$\sigma_{v,Ed}$  - equivalent stress     $\sigma_{Rd}$  - limit normal stress     $\tau_{Rd}$  - limit shear stress    U - utilization

### 3.5.3. weld between base plate and shear connector

design with direction oriented method acc. to clause 4.5.3.2

$$\sigma_{v,w,Ed} = (\sigma_{\perp}^2 + 3 \cdot \tau_{\perp}^2 + 3 \cdot \tau_{\parallel}^2)^{0.5}$$

$$f_{1,w,Rd} = f_u / (\beta_w \cdot \gamma_{M2})$$

$$f_{2,w,Rd} = 0.9 \cdot f_u / \gamma_{M2}$$

$$U = \max\{ \sigma_{v,w,Ed} / f_{1,w,Rd}, \sigma_{\perp} / f_{2,w,Rd} \}$$

connection designed with a full-size double fillet weld.

axial force transfer of 100 % by the weld.

minimum value of the weld thickness  $a_{min} = 8$  mm

LK	$a_{w,F1}$ mm	$a_{w,S}$ mm	$\sigma_{\perp}$ kN/cm <sup>2</sup>	$\tau_{\perp}$ kN/cm <sup>2</sup>	$\tau_{\parallel}$ kN/cm <sup>2</sup>	$\sigma_{v,w,Ed}$ kN/cm <sup>2</sup>	$f_{1,w,Rd}$ kN/cm <sup>2</sup>	$f_{2,w,Rd}$ kN/cm <sup>2</sup>	Maßgeb.	U
1	8	8	0.13	0.13	1.40	2.44	36.00	25.92	web	0.07
2	8	8	0.20	0.20	1.89	3.30	36.00	25.92	web	0.09
3	8	8	1.03	1.03	4.90	8.73	36.00	25.92	web	0.24
4	8	8	1.24	1.24	5.39	9.65	36.00	25.92	web	0.27

maximum weld thickness flange  $a_{w,F1,max} = 8$  mm

maximum weld thickness of the web  $a_{w,S,max} = 8$  mm

maximum utilization  $U = 0.27 < 1.00$

$a_{w,F1}$  - flange weld thickness     $a_{w,S}$  - web weld thickness     $a_w$  - weld thickness     $\sigma_{\perp}$  - normal stresses perpendicular to weld  
 $\tau_{\perp}$  - shear stresses perpendicular to weld     $\tau_{\parallel}$  - shear stresses parallel to weld    U - utilization

## 4. design calculation of foundation slab

### 4.1. partial safety factors for material

design situat.	$\gamma_c$	$\gamma_s$
permanent and transient	1.50	1.15

### 4.2. design values of reinforced concrete design

Die Mobilisierung des passive earth pressurees wird vernachlässigt.

#### 4.2.1. factorization of load case combinations

LK	design situat.	factorization
1	permanent and transient	Lf1
2	permanent and transient	1.35 · Lf1
3	permanent and transient	Lf1+1.5 · Lf2
4	permanent and transient	1.35 · Lf1+1.5 · Lf2

#### 4.2.2. column load

increasing factor for flex. mom.:  $\Delta M_{St,TH,II,0} = M_{St} \cdot 20\%$

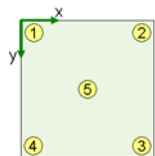
(for the consideration of increase of moments from non-linear effects)

LK	$N_{st,d}$ kN	$H_{x,St,d}$ kN	$H_{y,St,d}$ kN	$M_{x,St,d}$ kNm	$M_{y,St,d}$ kNm
1	200.00	0.00	30.00	60.00	0.00
2	270.00	0.00	40.50	81.00	0.00
3	350.00	0.00	105.00	195.00	0.00
4	420.00	0.00	115.50	216.00	0.00

### 4.3. base pressure

determination of base pressures assuming linear soil stresses and elimination of tension

stress in the corner points:  $\sigma_1$  to  $\sigma_4$ , stress in centroid:  $\sigma_5$



LK	$\sigma_1$ kN/m <sup>2</sup>	$\sigma_2$ kN/m <sup>2</sup>	$\sigma_3$ kN/m <sup>2</sup>	$\sigma_4$ kN/m <sup>2</sup>	$\sigma_5$ kN/m <sup>2</sup>
1	9.04	9.04	225.04	225.04	117.04
2	12.20	12.20	303.80	303.80	158.00
3	0.00	0.00	668.65	668.65	86.62
4	0.00	0.00	710.35	710.35	168.94

#### 4.4. Design calculation for bending

##### 4.4.1. longitudinal reinforcement in x-direction

reinforcement edge distance top/bottom  $h_{so}/h_{su} = 5.0/5.0$  cm

##### moments in design calculation sections

LK	x = 30.0 cm	x = 70.0 cm
	kNm	kNm
1	8.91	8.91
2	12.03	12.03
3	15.66	15.66
4	18.78	18.78

Design calculation for LK 4:  $\epsilon_o/\epsilon_u = -0.50/28.64\%$   $\min A_{s,u} = 1.2$  cm<sup>2</sup>

##### 4.4.2. longitudinal reinforcement in y-direction

reinforcement edge distance top/bottom  $h_{so}/h_{su} = 6.0/6.0$  cm

##### moments in design calculation sections

LK	y = 70.0 cm	y = 130.0 cm
	kNm	kNm
1	3.98	44.55
2	5.37	60.14
3	-4.41	126.14
4	-5.95	137.13

Design calculation for LK 4:  $\epsilon_o/\epsilon_u = 29.48/-0.41\%$   $\min A_{s,o} = 0.4$  cm<sup>2</sup>

Design calculation for LK 4:  $\epsilon_o/\epsilon_u = -2.67/29.88\%$   $\min A_{s,u} = 9.2$  cm<sup>2</sup>

$\epsilon_o/\epsilon_u$  - strains in extreme fibres (top/bottom)

#### 4.5. punching shear calculation

##### 4.5.1. action within the basic control perimeter

$$V_{Ed,crit} = \beta \cdot V_{Ed,red} / (u_{crit} \cdot d)$$

$$V_{Ed,red} = V_{Ed} - \Delta V_{Ed}$$

$$\Delta V_{Ed} = A_{crit} (\sigma_{Ed,gd,m} - g_{Ed,slab})$$

$$\beta = 1 + k \cdot M_{Ed} / V_{Ed} \cdot u_{crit} / W_{crit} \geq 1.10$$

$$W_{crit} = \int |e| dl \quad \text{mit } dl: \text{differential of perimeter} \\ e: \text{distance of } dl \text{ to axis of } M_{Ed}$$

##### coefficient for the calculation of shear stresses from moment action

(acc. to [2], table 6.1)

$$c_1/c_2 = 0.6/0.4 = 1.5 \Rightarrow k_x = 0.65$$

##### calculated values of basic control perimeter

LK	$a_{crit}$ cm	a/d	$u_{crit}$ m	$A_{crit}$ m <sup>2</sup>	$W_{crit,x}$ m <sup>2</sup>
1	19.1	0.56	3.20	0.738	1.0808
2	19.1	0.56	3.20	0.738	1.0808
3	19.8	0.57	3.25	0.760	1.1100
4	19.3	0.56	3.21	0.744	1.0880

##### decisive shear stress within the basic control perimeter

LK	$V_{Ed}$ kN	$\sigma_{Ed,gd,m}$ kN/m <sup>2</sup>	$\Delta V_{Ed}$ kN	$M_{Ed,x,Sp}$ kNm	$\beta$ -	$v_{Ed,crit}$ N/mm <sup>2</sup>
1	200.00	100.09	73.88	60.00	1.58	0.180
2	270.00	135.11	99.73	81.00	1.58	0.243
3	350.00	151.86	115.47	195.00	2.06	0.431
4	420.00	193.94	144.22	216.00	1.99	0.494

$\Delta V_{Ed}$  - resultant of ground pressure  $M_{Ed,x,Sp}/M_{Ed,y,Sp}$  - moments concerning centre of control perimeter

$\beta$  - load increase factor from eccentric load  $v_{Ed,crit}$  - decisive shear stress within the basic control perimeter

#### 4.5.2. Punching shear resistance within the basic control perimeter

$$V_{Rd,c} = C_{Rd,c} \cdot k (100 \cdot \rho_{l,tension} \cdot f_{ck})^{1/3} \cdot 2 \cdot d/a \geq v_{min} \cdot 2 \cdot d/a \text{ [N/mm}^2\text{]}$$

$$C_{Rd,c} = 0.15/\gamma_c$$

$$k = 1 + \sqrt{200/d} \leq 2.0 \text{ with } d \text{ [mm]}$$

$$\rho_{l,tension,max} = \text{minimum from } (0.02, 0.5 \cdot f_{cd}/f_{yd})$$

$$\rho_{l,tension} = \sqrt{(\rho_{lx,tension} \cdot \rho_{ly,tension})} \leq \rho_{l,tension,max}$$

$$v_{min} = 0.0525/\gamma_c \cdot k^{3/2} \cdot f_{ck}^{1/2} \text{ for } d \leq 600 \text{ mm}$$

mean effective depth

$$d_m = (35 + 34)/2 = 34.5 \text{ cm}$$

scale factor

$$k = 1 + \sqrt{200/345} = 1.76 < 2$$

longitudinal reinf. ratio of the anchored tension reinf.

mean of the tension reinforcement to the distance 3d from the column

$$a_{s,x,3d} = 1.2/2 = 0.59 \text{ cm}^2/\text{m}$$

$$a_{s,y,3d} = 9.2/1 = 9.19 \text{ cm}^2/\text{m}$$

$$\rho_{lx,tension} = 0.59/35 \cdot 10^{-2} = 0.00017$$

$$\rho_{ly,tension} = 9.19/34 \cdot 10^{-2} = 0.0027$$

$$\rho_{l,tension} = \sqrt{0.00017 \cdot 0.0027} = 0.00068$$

punching shear resistance without shear reinforcement

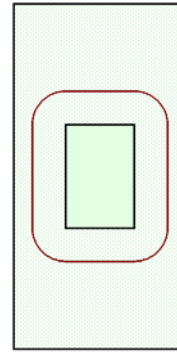
$$C_{Rd,c} = 0.15/1.5 = 0.1$$

$$\rho_{l,tension,max} = \text{minimum from } (0.02, 0.5 \cdot 17/434.78) = 0.0195 > 0.0007$$

$$v_{min} \cdot 2 \cdot d/a = 0.0525/1.5 \cdot 1.76^{3/2} \cdot 30^{0.5} \cdot 2 \cdot 34.5/19.3 = 1.6 \text{ N/mm}^2$$

$$V_{Rd,c} = 0.1 \cdot 1.76 \cdot (100 \cdot 0.00068 \cdot 30)^{1/3} \cdot 2 \cdot 34.5/19.3 = 0.796 \text{ N/mm}^2 < 1.6 \text{ N/mm}^2 \Rightarrow V_{Rd,c} = 1.6 \text{ N/mm}^2$$

0.494 N/mm<sup>2</sup> < 1.6 N/mm<sup>2</sup> ⇒ no additional reinforcement required



### 5. External stability - verification of design resistance (ULS)

#### 5.1. partial safety factors auf der actionsseite

acc. to [3] table A 2.1

#### 5.2. partial safety factors auf der resistance side

acc. to [3] tables A 2.2 and A 2.3

#### 5.3. design values overturning (EQU)

Die Mobilisierung des passive earth pressurees wird vernachlässigt.

##### 5.3.1. factorization of load case combinations

LK	design situat.	factorization
1	BS-P	0.9 · Lf1
2	BS-P	1.1 · Lf1
3	BS-P	0.9 · Lf1 + 1.5 · Lf2
4	BS-P	1.1 · Lf1 + 1.5 · Lf2

##### 5.3.2. column load

LK	N <sub>St,d</sub> kN	H <sub>x,St,d</sub> kN	H <sub>y,St,d</sub> kN	M <sub>x,St,d</sub> kNm	M <sub>y,St,d</sub> kNm
1	180.00	0.00	27.00	45.00	0.00
2	220.00	0.00	33.00	55.00	0.00
3	330.00	0.00	102.00	157.50	0.00
4	370.00	0.00	108.00	167.50	0.00

#### 5.4. verification against overturning (EQU)

no destabilising loading ⇒ verification is not necessary.

#### 5.5. design values base failure (GEO-2)

the assumed mobilised passive earth pressure is  $e_{phg,mob} = 0.50 \cdot e_{phg}$ .

##### 5.5.1. factorization of load case combinations

LK	design situat.	factorization
1	BS-P	Lf1
2	BS-P	1.35 · Lf1
3	BS-P	Lf1 + 1.5 · Lf2
4	BS-P	1.35 · Lf1 + 1.5 · Lf2

##### 5.5.2. column load

LK	N <sub>St,d</sub> kN	H <sub>x,St,d</sub> kN	H <sub>y,St,d</sub> kN	M <sub>x,St,d</sub> kNm	M <sub>y,St,d</sub> kNm
1	200.00	0.00	30.00	50.00	0.00
2	270.00	0.00	40.50	67.50	0.00
3	350.00	0.00	105.00	162.50	0.00
4	420.00	0.00	115.50	180.00	0.00

associated characteristic values



LK	N <sub>st,k</sub> kN	H <sub>x,St,k</sub> kN	H <sub>y,St,k</sub> kN	M <sub>x,St,k</sub> kNm	M <sub>y,St,k</sub> kNm
1	200.00	0.00	30.00	50.00	0.00
2	200.00	0.00	30.00	50.00	0.00
3	300.00	0.00	80.00	125.00	0.00
4	300.00	0.00	80.00	125.00	0.00

## 5.6. verification of safety against base failure

### 5.6.1. loading and substituting dimensions

LK	N <sub>0,k</sub> kN	M <sub>0,x,k</sub> kNm	M <sub>0,y,k</sub> kNm	a'	b'	H <sub>a',k</sub> kN	H <sub>b',k</sub> kN
1	234.08	61.82	0.00	1.47	1.00	28.98	0.00
2	234.08	61.82	0.00	1.47	1.00	28.98	0.00
3	334.08	156.82	0.00	1.06	1.00	78.98	0.00
4	334.08	156.82	0.00	1.06	1.00	78.98	0.00

### 5.6.2. decisive soil parameters

determination of the decisive values by method of weighted average

values beyond the base to top edge of soil:  $\gamma_1, \varphi_1, c_1$

values below the base up to depth ( $d_s$ ) of the sliding clod:  $\gamma_2, \varphi_2, c_2$

LK	$\gamma_1$ kN/m <sup>3</sup>	$\varphi_1$ °	c <sub>1</sub> kN/m <sup>2</sup>	d <sub>s</sub> m	$\gamma_2$ kN/m <sup>3</sup>	$\varphi_2$ °	c <sub>2</sub> kN/m <sup>2</sup>
1	20.00	35.00	---	1.90	19.04	35.00	---
2	20.00	35.00	---	1.90	19.04	35.00	---
3	20.00	35.00	---	1.90	19.04	35.00	---
4	20.00	35.00	---	1.90	19.04	35.00	---

### 5.6.3. values of design resistance, shape, load inclination and depth

basic values of design resistance values  $N_{b0}, N_{d0}, N_{c0}$  acc. to [4]

shape factors  $v_b, v_d, v_c$  acc. to [4], tab.2

load inclination factors  $i_b, i_d, i_c$  acc. to [4], tab.3

LK	N <sub>b0</sub>	N <sub>d0</sub>	N <sub>c0</sub>	v <sub>b</sub>	v <sub>d</sub>	v <sub>c</sub>	i <sub>b</sub>	i <sub>d</sub>	i <sub>c</sub>
1	22.61	33.30	---	0.796	1.390	---	0.728	0.831	---
2	22.61	33.30	---	0.796	1.390	---	0.728	0.831	---
3	22.61	33.30	---	0.717	1.541	---	0.512	0.670	---
4	22.61	33.30	---	0.717	1.541	---	0.512	0.670	---

### 5.6.4. ultimate load and allowable load

characteristic design bearing capacity  $R_{n,k} = a' \cdot b' \cdot (\gamma_2 \cdot b' \cdot N_{b0} \cdot v_b \cdot i_b + \gamma_1 \cdot t \cdot N_{d0} \cdot v_d \cdot i_d + c_2 \cdot N_{c0} \cdot v_c \cdot i_c)$

design value of resistance  $R_{n,d} = R_{n,k} / \gamma_{Gr}$

the degree of utilization is  $\mu = N_d / R_{n,d}$

LK	R <sub>n,k</sub> kN	$\gamma_{R,v}$ -	R <sub>n,d</sub> kN	N <sub>d</sub> kN	$\mu$ -
1	1272.19	1.40	908.71	234.08	0.26
2	1272.19	1.40	908.71	316.01	0.35
3	751.09	1.40	536.49	384.08	0.72
4	751.09	1.40	536.49	466.01	<b>0.87</b>

$\mu_{max} = 0.87 < 1.0 \Rightarrow$  design bearing capacity sufficient

## 5.7. design values slippage (GEO-2)

the assumed mobilised passive earth pressure is  $e_{phg,mob} = 1.00 \cdot e_{phg}$ .

design values of applied loads see base failure.

## 5.8. verification of safety against sliding

slip resistance in case of consolidated soil  $R_{t,k} = N_{0,k} \cdot \tan(\delta_s)$

design value of slip resistance  $R_{t,d} = R_{t,k} / \gamma_{R,h}$

design value of mobilised passive earth pressure  $E_{p,d} = E_{p,k,mob} / \gamma_{R,e}$

the degree of utilization is  $\mu = (R_{t,d} + E_{p,d}) / H_{Res,d}$

angle of base friction (for raue base area)  $\delta_s = 35.0^\circ$

LK	N <sub>0,k</sub> kN	R <sub>t,k</sub> kN	$\gamma_{R,h}$ -	$\gamma_{R,e}$ -	R <sub>t,d</sub> kN	E <sub>p,d</sub> kN	H <sub>Res,d</sub> kN	$\mu$ -
1	234.08	163.90	1.10	1.40	149.00	1.46	30.00	0.20
2	234.08	163.90	1.10	1.40	149.00	1.46	40.50	0.27
3	334.08	233.93	1.10	1.40	212.66	1.46	105.00	0.49
4	334.08	233.93	1.10	1.40	212.66	1.46	115.50	<b>0.54</b>

$\mu_{max} = 0.54 < 1.0 \Rightarrow$  slip resistance sufficient

## 6. External stability - verification of serviceability

### 6.1. design values limitation of gapping joint under permanent load

Die Mobilisierung des passive earth pressurees wird vernachlässigt.

#### 6.1.1. factorization of load case combinations

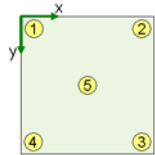
LK	factorization
1	Lf1

#### 6.1.2. column load

LK	N <sub>St,d</sub> kN	H <sub>x,St,d</sub> kN	H <sub>y,St,d</sub> kN	M <sub>x,St,d</sub> kNm	M <sub>y,St,d</sub> kNm
1	200.00	0.00	30.00	50.00	0.00

#### 6.1.3. base pressure

determination of base pressures assuming linear soil stresses and elimination of tension  
stress in the corner points:  $\sigma_1$  to  $\sigma_4$ , stress in centroid:  $\sigma_5$



LK	$\sigma_1$ kN/m <sup>2</sup>	$\sigma_2$ kN/m <sup>2</sup>	$\sigma_3$ kN/m <sup>2</sup>	$\sigma_4$ kN/m <sup>2</sup>	$\sigma_5$ kN/m <sup>2</sup>
1	24.04	24.04	210.04	210.04	117.04

## 6.2. limitation of gapping joint under permanent load

internal forces and moments in centroid of foundation base:  $N_{0,k} = 234.08$  kN

$$M_{0,x,k} = 62.00 \text{ kNm}$$

$$M_{0,y,k} = 0.00 \text{ kNm}$$

resultant eccentricity:  $e_x = 0.00$  m

$$e_y = 0.26 \text{ m}$$

$$e_x/b_x + e_y/b_y = 0.13 < 1/6$$

⇒ the resultant is located in the 1. core area

sc. no emerge of a gapping joint due to permanent load.

## 6.3. design values limitation of gapping joint under total load

Die Mobilisierung des passive earth pressurees wird vernachlässigt.

#### 6.3.1. factorization of load case combinations

LK	factorization
1	Lf1
2	Lf1+Lf2

#### 6.3.2. column load

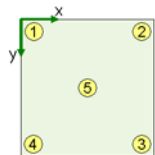
increasing factor for flex. mom.:  $\Delta M_{St,TH.II.0} = M_{St} \cdot -200\%$

(for the consideration of increase of moments from non-linear effects)

LK	N <sub>St,d</sub> kN	H <sub>x,St,d</sub> kN	H <sub>y,St,d</sub> kN	M <sub>x,St,d</sub> kNm	M <sub>y,St,d</sub> kNm
1	200.00	0.00	30.00	50.00	0.00
2	300.00	0.00	80.00	125.00	0.00

#### 6.3.3. base pressure

determination of base pressures assuming linear soil stresses and elimination of tension  
stress in the corner points:  $\sigma_1$  to  $\sigma_4$ , stress in centroid:  $\sigma_5$



LK	$\sigma_1$ kN/m <sup>2</sup>	$\sigma_2$ kN/m <sup>2</sup>	$\sigma_3$ kN/m <sup>2</sup>	$\sigma_4$ kN/m <sup>2</sup>	$\sigma_5$ kN/m <sup>2</sup>
1	24.04	24.04	210.04	210.04	117.04
2	0.00	0.00	420.18	420.18	155.94

## 6.4. limitation of gapping joint under total load

LK	$N_{0,k}$ kN/m	$M_{0,x,k}$ kNm/m	$M_{0,y,k}$ kNm/m	$e_x$ m	$e_y$ m	$(e_x/b_x)^2 + (e_y/b_y)^2$
1	234.08	62.00	0.00	0.00	0.26	0.018
2	334.08	157.00	0.00	0.00	0.47	0.055

$$((e_x/b_x)^2 + (e_y/b_y)^2)_{\max} = 0.055 < 1/9$$

⇒ the decisive resultant is located in the 2. core area,

sc. no gapping joint beyond centroid.

## 6.5. verification against displacement in base area

the verification is rated as successful, if the passive earth pressure remains unconsidered in the verification of safety against sliding (s.a.).

LK	$N_{0,k}$ kN	$R_{t,k}$ kN	$\gamma_{R,h}$ -	$R_{t,d}$ kN	$H_{Res,d}$ kN	$\mu$ -
1	234.08	163.90	1.10	149.00	30.00	0.20
2	234.08	163.90	1.10	149.00	40.50	0.27
3	334.08	233.93	1.10	212.66	105.00	0.49
4	334.08	233.93	1.10	212.66	115.50	<b>0.54</b>

$\mu_{max} = 0.54 < 1.0 \Rightarrow$  verification against displacement in base area successful

## 6.6. design values settlement

Die Mobilisierung des passive earth pressurees wird vernachlässigt.

### 6.6.1. factorization of load case combinations

LK	factorization
1	Lf1
2	Lf1+Lf2

### 6.6.2. column load

LK	$N_{St,d}$ kN	$H_{x,St,d}$ kN	$H_{y,St,d}$ kN	$M_{x,St,d}$ kNm	$M_{y,St,d}$ kNm
1	200.00	0.00	30.00	50.00	0.00
2	300.00	0.00	80.00	125.00	0.00

## 6.7. settlements

determination of settlement by use of closed formulas acc. to [5]

allowable maximum settlement perm  $s_{max} = 5.0$  cm

allowable obliquity about the x-axis perm  $\alpha_x = 0.5^\circ$

allowable obliquity about the y-axis perm  $\alpha_y = 0.5^\circ$

### 6.7.1. determination from settlement causing contact pressure and limiting depth

mean settlement causing contact pressure  $\sigma_0' = \sigma_0 - \sigma_a$ , if  $2\sigma_a > \sigma_0$  then  $\sigma_0' = \sigma_0$

the limiting depth  $d_s$  results from  $d_s = z$ , if  $\sigma_B(z) = 0.2\sigma_0'(z)$  below significant point.

unloading from excavation due to foundation depth  $\sigma_a = 16.00$  kN/m<sup>2</sup>

LK	$N_{0,k}$ kN	$M_{0,x,k}$ kNm	$M_{0,y,k}$ kNm	$\sigma_0$ kN/m <sup>2</sup>	$\sigma_0'$ kN/m <sup>2</sup>	$d_s$ m
1	234.08	62.00	0.00	117.04	101.04	2.41
2	334.08	157.00	0.00	167.04	151.04	2.95

### 6.7.2. determination of settlement values and settlement parts per soil stratum

coefficient f for settlement below significant point acc. to [6], vol. 2, tab. 4

coefficients  $f_x/f_y$  for obliquity of a rigid foundation acc. to [7], fig. 19

settlement parts from central load  $s_{m,i} = \sigma_0' \cdot b_y \cdot (f_i - f_{i-1}) / E_{m,i}$

settlement parts from  $M_{0,y}$   $s_{x,i} = b_x/2 \cdot M_{0,y} / (E_{m,i} \cdot b_y \cdot b_x^2) \cdot (f_{x,i} - f_{x,i-1})$

settlement parts from  $M_{0,x}$   $s_{y,i} = b_y/2 \cdot M_{0,x} / (E_{m,i} \cdot b_x \cdot b_y^2) \cdot (f_{y,i} - f_{y,i-1})$

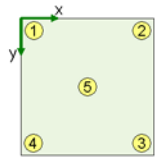
LK 1:	level	z	f	$f_x$	$f_y$	$S_m$	$S_x$	$S_y$
$\sigma_0' = 101.04$ kN/m <sup>2</sup>	m	m	-	-	-	cm	cm	cm
$M_{0,x} = 62.00$ kNm	2.50	1.70	0.366	4.296	2.930	0.09	0.00	0.06
$M_{0,y} = 0.00$ kNm	3.21	2.41	0.418	4.408	3.075	0.01	0.00	0.00

LK 2:	level	z	f	$f_x$	$f_y$	$S_m$	$S_x$	$S_y$
$\sigma_0' = 151.04$ kN/m <sup>2</sup>	m	m	-	-	-	cm	cm	cm
$M_{0,x} = 157.00$ kNm	2.50	1.70	0.366	4.296	2.930	0.14	0.00	0.14
$M_{0,y} = 0.00$ kNm	3.75	2.95	0.444	4.409	3.076	0.03	0.00	0.01

### 6.7.3. resultant settlements and obliquity per LK

$s_1 = \Sigma(s_{m,i} + s_{x,i} - s_{y,i})$   $s_2 = \Sigma(s_{m,i} - s_{x,i} - s_{y,i})$   $s_3 = \Sigma(s_{m,i} - s_{x,i} + s_{y,i})$   $s_4 = \Sigma(s_{m,i} + s_{x,i} + s_{y,i})$   $s_5 = \Sigma s_{m,i}$

$\tan \alpha_x = 2 \cdot \Sigma s_{y,i} / b_y$   $\tan \alpha_y = 2 \cdot \Sigma s_{x,i} / b_x$



LK	$s_1$ cm	$s_2$ cm	$s_3$ cm	$s_4$ cm	$s_5$ cm	$S_{max}$ cm	$\alpha_x$ °	$\alpha_y$ °
1	0.0	0.0	0.2	0.2	0.1	0.2	0.0	<b>0.0</b>
2	0.0	0.0	0.3	0.3	0.2	<b>0.3</b>	<b>0.1</b>	0.0

$\max S_{max} = 0.3 < 5.0$  cm  $\max |\alpha_x| = 0.1^\circ < 0.5^\circ$   $\max |\alpha_y| = 0.0^\circ < 0.5^\circ$

$\Rightarrow$  allowable settlement and obliquity kept

$N_0$  - normal force in foundation joint  $M_0$  - moment load in centroid of foundation joint

$a'/b'$  - substituting widths due to eccentric load with  $a' > b'$   $H_a/H_b$  - horizontal loads in direction of the corresponding widths

$t$  - anchoring depth  $\sigma_0$  - mean normal soil stress  $\sigma_B$  - soil stress from structural load



$\sigma_0$  - overburden stress from soil own weight     $d_s$  - limiting depth resp. thickness of compressible stratum below base of foundation  
z - depth from foundation foot

## 7. summary

◦ the allowable tension force of one or more anchors is exceeded.

design calculation not successful!

### Literatur and Normen:

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