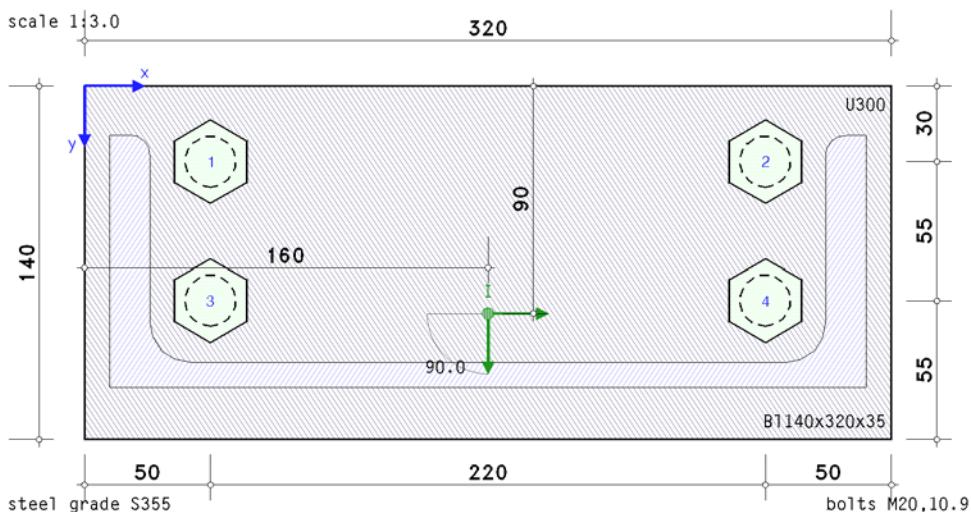


**bolted end-plate connection**

EC 3-1-8 (12.10), NA: Deutschland

**steel grade**

steel grade S355

**bolts**

bolt class 10.9, bolt size M20, thread included in the shear plane

**connection**end-plate: thickness  $t_p = 35.0$  mm, width  $b_p = 320.0$  mm, length  $l_p = 140.0$  mm

beam: section U300

rotation of cross-section arround section centroid  $\beta = 90.0^\circ$ beam-end-plate: surrounding fillet weld, weld thickness  $a = 10.0$  mmcoordinates of centroid of beam section bei  $x_p = 160.0$  mm,  $y_p = 90.0$  mmcoordinates of beam centroid on end-plate  $x_s = 160.0$  mm,  $y_s = 90.0$  mm**bolts:**

uniform arrangement of bolts, 2 vertical and 2 horizontal rows

edge distances top  $e_o = 30.0$  mm, bottom  $e_u = 55.0$  mmdistances between bolts  $p_{x,1-2} = 220.0$  mmedge distances left  $e_l = 50.0$  mm, right  $e_r = 50.0$  mmdistances between bolts  $p_{y,1-2} = 55.0$  mm**calculation**

verification:

calculation and verification of internal forces and moments (FEM)

verification of end-plate with the plastic method

verification of beam section with the plastic method

verification of welds with the directional method

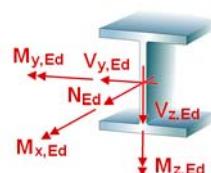
verification of bolts, check of distances

**FEM-calculation:**bolts are plastically calculated, spring constant of bolts  $c_f = 7433.6$  kN/cmplastic limit force  $F_{t,f} = f_{t,f} F_{t,Rd} = 167.6$  kN,  $f_{t,f} = 0.950$ ,  $F_{t,Rd} = 176.4$  kN, effective elongation at failure  $\epsilon_{t,f} = 4.5\%$  without preloading ( $F_{p,C} = 0$ )effective foundation modulus of end plate  $c_b = 12000.0$  kN/cm<sup>3</sup>number / dimension of finite elements each direction  $n_x / \Delta x = 32 / 10.0$  mm,  $n_y / \Delta y = 20 / 7.0$  mm

max. 50 iteration steps (tolerance limit 5%)

**internal forces and moments**

Lk	N <sub>Ed</sub> kN	M <sub>y,Ed</sub> kNm	V <sub>z,Ed</sub> kN	M <sub>z,Ed</sub> kNm	V <sub>y,Ed</sub> kN	M <sub>x,Ed</sub> kNm
1	-33.5	81.2	-21.2	-6.1	-4.4	-0.9
2	0.3	4.7	1.3	-5.7	2.4	-0.0
3	-33.2	80.9	-21.4	-5.8	-4.2	-0.9
4	0.1	4.9	1.5	-5.9	2.3	-0.0
5	-7.8	7.8	-5.1	14.0	5.8	-0.1
6	-26.5	71.3	-17.8	-15.7	-8.5	-0.9
7	-28.3	69.2	-20.0	-7.7	-5.4	-0.9
8	-3.4	13.1	0.5	-4.6	3.1	0.0
9	-25.6	72.3	-16.6	-18.9	-7.0	-0.9
10	-30.8	84.4	-17.8	-17.3	-6.0	-0.9
11	-4.1	-0.6	-4.3	12.9	5.1	-0.1



## partial safety factors for material

resistance of cross-sections  $\gamma_{M0} = 1.00$

resistance of bolts, welds, plates in bearing  $\gamma_{M2} = 1.25$

## Calculation

### utilizations

Lk	$U_p$	$U_\sigma$	$U_b$	$U_{wt}$	$U_{t,s}$	$U_{vt,s}$	$U_{b,s}$	$U_q$	$U_{c/t}$	$U_w$	U
1	0.380	0.353	0.380	0.456	0.950	0.695	0.039	0.526	0.353	0.570	0.950*
2	0.101	0.041	0.101	0.038	0.249	0.185	0.003	0.133	0.200	0.192	0.249
3	0.378	0.343	0.378	0.441	0.950	0.695	0.039	0.519	0.349	0.559	0.950*
4	0.104	0.043	0.104	0.039	0.260	0.193	0.003	0.139	0.204	0.199	0.260
5	0.202	0.144	0.202	0.056	0.371	0.278	0.009	0.306	0.281	0.450	0.450
6	0.527	0.460	0.527	0.599	0.950	0.696	0.038	0.660	0.614	0.804	0.950*
7	0.310	0.276	0.310	0.332	0.950	0.688	0.035	0.501	0.348	0.558	0.950*
8	0.084	0.057	0.084	0.050	0.331	0.243	0.003	0.152	0.206	0.200	0.331
9	0.629	0.545	0.629	0.733	0.950	0.699	0.039	0.726	0.614	0.905	0.950*
10	0.712	0.666	0.712	0.921	0.950	0.707	0.045	0.752	0.614	0.916	0.950*
11	0.171	0.111	0.171	0.044	0.290	0.225	0.008	0.254	0.274	0.386	0.386

Up: utilization of end-plate;  $U_\sigma$ : utilization of end-plate due to stress;  $U_p$ : utilization of end-plate due to compression by contact

$U_{wt,s}$ : utilization of bolts due to elongation;  $U_{t,s}$ : utilization of bolts due to tension;  $U_{vt,s}$ : utilization of bolts due to shear in tension

$U_{b,s}$ : utilization of bolts due to bearing resistance;  $U_q$ : stress utilization of beam;  $U_{c/t}$ : c/t-utilization of beam

$U_w$ : utilization of welds; U: total utilization

\*) maximum utilization

## Final Result

maximum utilization [Lk 1] max U = 0.950 < 1 ok.

verification succeeded

## Regulations

DIN EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;

Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010

DIN EN 1990/NA, Nationaler Anhang zur DIN EN 1990, Ausgabe Dezember 2010

DIN EN 1993-1-1, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;

Deutsche Fassung EN 1993-1-1:2005 + AC:2009, Ausgabe Dezember 2010

DIN EN 1993-1-1/NA, Nationaler Anhang zur DIN EN 1993-1-1, Ausgabe Dezember 2010

DIN EN 1993-1-8, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-8: Bemessung von Anschlüssen;

Deutsche Fassung EN 1993-1-8:2005 + AC:2009, Ausgabe Dezember 2010

DIN EN 1993-1-8/NA, Nationaler Anhang zur DIN EN 1993-1-8, Ausgabe Dezember 2010

## Detailed edition of Lk 1 (decisive)

Lk 1:  $N_{Ed} = -33.5 \text{ kN}$ ,  $M_{y,Ed} = 81.2 \text{ kNm}$ ,  $V_{z,Ed} = -21.2 \text{ kN}$ ,  $M_{z,Ed} = -6.1 \text{ kNm}$ ,  $V_y$

### end-plate

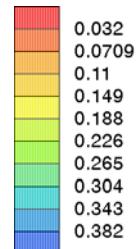
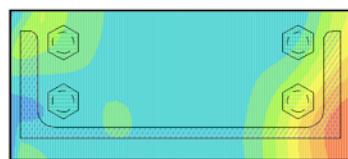
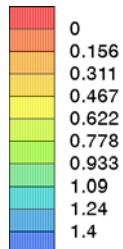
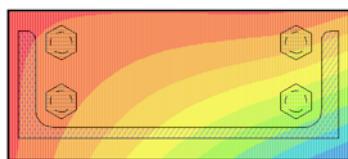
design values:  $N = -33.47 \text{ kN}$ ,  $M_y = 81.25 \text{ kNm}$ ,  $M_z = -6.13 \text{ kNm}$

deformations  $u_z$  [mm], lifting off positive

min  $u_z = -0.04 \text{ mm}$ , max  $u_z = 1.40 \text{ mm}$

utilization of end-plate  $U_p$

min  $U_p = 0.032$ , max  $U_p = 0.380$



## utilization of end-plate

Kno	x mm	y mm	uz mm	U <sub>σ</sub>	U <sub>b</sub>	U <sub>p</sub>
19	0.0	126.0	-0.041	0.292	0.380	0.380
693	320.0	140.0	1.400	0.036	---	0.036

x,y: node coordinates; u<sub>z</sub>: deformations (lifting off positive); U<sub>σ</sub>: utilization due to moment with shear force; U<sub>b</sub>: utilization due to compression by contact  
U<sub>p</sub>: utilization of end-plate

## tension force of bolts

	x mm	y mm	w <sub>t</sub> mm	F <sub>t</sub> kN	ε <sub>wt</sub> %	U <sub>wt</sub>
1	50.0	30.0	0.022	16.57	0.064	0.014
2	270.0	30.0	0.248	148.88	0.708	0.157
3	50.0	85.0	0.096	71.71	0.276	0.061
4	270.0	85.0	0.718	167.58	2.050	0.456

x,y: bolt coordinates; w<sub>t</sub>: deformation (tension positive); F<sub>t</sub>: bolt force; ε<sub>wt</sub>: elongation  
U<sub>wt</sub>: utilization due to elongation

utilization of end-plate [node 20] U<sub>max</sub> = 0.380 < 1 **ok.**

utilization of bolts due to elongation [bolt 4] U<sub>max</sub> = 0.456 < 1 **ok.**

## bolts

design values: max F<sub>t</sub> = 167.58 kN, V<sub>z</sub> = -21.16 kN, V<sub>y</sub> = -4.35 kN, M<sub>x</sub> = -0.92 kNm

### verification of bolts

U<sub>p</sub>: utilization due to tension/punching shear failure, U<sub>vt</sub>: utilization due to shear in tension, U<sub>b</sub>: utilization due to bearing resistance, U: utilization of bolts

bolt 1	U <sub>tp,1</sub> = 0.094	U <sub>vt,1</sub> = 0.157	U <sub>b,1</sub> = 0.039	U <sub>1</sub> = 0.157
bolt 2	U <sub>tp,2</sub> = 0.844	U <sub>vt,2</sub> = 0.654	U <sub>b,2</sub> = 0.022	U <sub>2</sub> = 0.844
bolt 3	U <sub>tp,3</sub> = 0.407	U <sub>vt,3</sub> = 0.360	U <sub>b,3</sub> = 0.024	U <sub>3</sub> = 0.407
bolt 4	U <sub>tp,4</sub> = 0.950	U <sub>vt,4</sub> = 0.695	U <sub>b,4</sub> = 0.006	U <sub>4</sub> = 0.950
total Max:	U <sub>tp</sub> = 0.950	U <sub>vt</sub> = 0.695	U <sub>b</sub> = 0.039	U = 0.950 < 1 <b>ok.</b>

utilization of bolts [bolt 4] U<sub>max</sub> = 0.950 < 1 **ok.**

## beam

plastic cross-sectional check for N = -33.47 kN, M<sub>y</sub> = 81.25 kNm, V<sub>z</sub> = -21.16 kN,

M<sub>z</sub> = -6.13 kNm, V<sub>y</sub> = -4.35 kN, M<sub>x</sub> = -0.92 kNm

valid normal-/shear stress: zul σ<sub>Rd</sub> = 35.50 kN/cm<sup>2</sup>, zul τ<sub>Rd</sub> = 20.50 kN/cm<sup>2</sup>

top flange: shear force V<sub>o</sub> = -4.66 kN, torsion T<sub>po</sub> = -0.35 kNm, shear stress τ<sub>o</sub> = 2.98 kN/cm<sup>2</sup> ⇒ U<sub>τ,o</sub> = 0.145  
flange bending M<sub>σ,o</sub> = -12.99 kNm, bending stress σ<sub>o</sub> = 17.95 kN/cm<sup>2</sup> ⇒ U<sub>σ,o</sub> = 0.511  
design resistance forces N<sub>max,o</sub> = 22.94 kN, N<sub>min,o</sub> = -423.59 kN

bottom flange: shear force V<sub>u</sub> = 0.30 kN, torsion T<sub>pu</sub> = -0.35 kNm, shear stress τ<sub>u</sub> = 2.95 kN/cm<sup>2</sup> ⇒ U<sub>τ,u</sub> = 0.144  
flange bending M<sub>σ,u</sub> = 6.04 kNm, bending stress σ<sub>u</sub> = 8.35 kN/cm<sup>2</sup> ⇒ U<sub>σ,u</sub> = 0.238  
design resistance forces N<sub>max,u</sub> = 335.40 kN, N<sub>min,u</sub> = -154.40 kN

web: shear force V<sub>s</sub> = -21.16 kN, torsion T<sub>ps</sub> = -0.23 kNm, shear stress τ<sub>s</sub> = 2.03 kN/cm<sup>2</sup> ⇒ U<sub>τ,s</sub> = 0.099  
design resistance forces N<sub>max,s</sub> = 946.71 kN, N<sub>min,s</sub> = -946.71 kN

main bending: axial force N = -33.47 kN, design resistance forces N<sub>max</sub> = 1305.04 kN, N<sub>min</sub> = -1524.70 kN ⇒ U<sub>N</sub> = 0.022  
moment M<sub>y</sub> = 81.25 kNm, design resistance moments M<sub>y,max</sub> = 170.99 kNm, M<sub>y,min</sub> = -87.93 kNm ⇒ U<sub>M,y</sub> = 0.475

total (possibly due to load increase): max U = 0.526 < 1 **ok.**

utilizations: design resistance U<sub>σ</sub> = 0.526 < 1 **ok.**, c/t-ratio U<sub>c/t</sub> = 0.353 < 1 **ok.**

utilization of beam max(U<sub>σ</sub>, U<sub>c/t</sub>) = 0.526 < 1 **ok.**

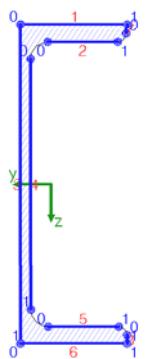
## welds

design values: N = -33.47 kN, M<sub>y</sub> = 81.25 kNm, V<sub>z</sub> = -21.16 kN, M<sub>z</sub> = -6.13 kNm,

V<sub>y</sub> = -4.35 kN, M<sub>x</sub> = -0.92 kNm

weld 3: weld thickness a = 10.0 mm > a<sub>max</sub> = t<sub>min</sub> = 7.1 mm **!!**

weld 4: weld thickness a = 10.0 mm > a<sub>max</sub> = t<sub>min</sub> = 7.1 mm **!!**



weld 1:  $a_w = 10.0 \text{ mm}$   $l_w = 100.0 \text{ mm}$   
weld 2:  $a_w = 10.0 \text{ mm}$   $l_w = 66.0 \text{ mm}$   
weld 3:  $a_w = 10.0 \text{ mm}$   $l_w = 300.0 \text{ mm}$   
weld 4:  $a_w = 10.0 \text{ mm}$   $l_w = 236.0 \text{ mm}$   
weld 5:  $a_w = 10.0 \text{ mm}$   $l_w = 66.0 \text{ mm}$   
weld 6:  $a_w = 10.0 \text{ mm}$   $l_w = 100.0 \text{ mm}$   
weld 7:  $a_w = 10.0 \text{ mm}$   $l_w = 8.0 \text{ mm}$   
weld 8:  $a_w = 10.0 \text{ mm}$   $l_w = 8.0 \text{ mm}$

Max:  $\sigma_{1,w,Ed} = 24.81 \text{ kN/cm}^2 < f_{1,w,Rd} = 43.56 \text{ kN/cm}^2$ ,  
 $\sigma_{2,w,Ed} = 12.40 \text{ kN/cm}^2 < f_{2,w,Rd} = 35.28 \text{ kN/cm}^2 \Rightarrow U_w = 0.570 < 1 \text{ ok.}$

utilization of welds  $U_{\max} = 0.570 < 1 \text{ ok.}$

utilization Lk 1  $U_{\max} = 0.950 < 1 \text{ ok.}$