

# POS. 18: WAGENKNECHT BD.2, BSP.11.10.6

## detailed problems acc. to Eurocode 3

EC 3-1-5 (12.10), NA: Deutschland

### steel grade

steel grade S 235

### cross-section

buckling field: thickness  $t = 10.0$  mm, width  $b = 1698.0$  mm

longitudinal stiffeners: number  $n_{st} = 2$

section L100X65X9

distance of the first stiffener to the top edge of plate  $d_{st,0} = 566.0$  mm

constant distance of stiffeners  $d_{st} = 566.0$  mm

transverse stiffeners to limit the buckling field:

section parameters (T-section):

$h = 260.0$  mm,  $t_w = 10.0$  mm,  $b_f = 100.0$  mm,  $t_f = 10.0$  mm

### parameters

length of buckling field  $a = 345.0$  cm

method of reduced stresses

verification in beam field

calculation of buckling factors with 4H-tool

### loading

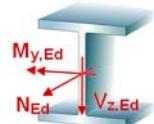
internal forces and moments referring to the stiffened cross-section:

Lk 1:  $N_{Ed} = -2182.0$  kN  $V_{Ed} = 687.0$  kN

### partial safety factors for material

resistance of cross-sections  $\gamma_{M0} = 1.00$

resistance of members in stability failure  $\gamma_{M1} = 1.10$

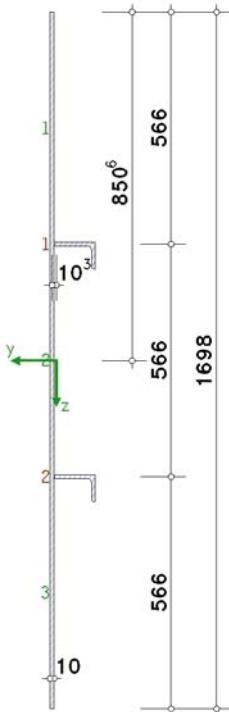


## verifications of buckling resistance

assumption: flange induced web buckling is excluded.

assumption: local buckling of stiffeners is excluded.

assumption: transverse stiffeners serve as rigid support of the plated panel.



## Lk 1:

### method of reduced stresses

EC 3-convention, compressive stresses positive  
shear distortions are ignored.

cross-sectional properties:  $A = 198.20 \text{ cm}^2$ ,  $z_s = 850.6 \text{ mm}$ ,  $I_y = 430845.31 \text{ cm}^4$ ,  $y_s = 10.3 \text{ mm}$ ,  $I_z = 1546.56 \text{ cm}^4$   
maximum/minimum stresses:  $\sigma_o = 110.1 \text{ N/mm}^2$ ,  $\sigma_u = 110.1 \text{ N/mm}^2$ ,  $\tau = 40.5 \text{ N/mm}^2$

### buckling factors (4H-tool)

web:  $\alpha_{cr} = 1.948$ ,  $\alpha_{cr,1} = 2.024$ ,  $\alpha_{cr,2} = 2.024$ ,  $\alpha_{cr,3} = 2.024$

### reduced stresses

#### single buckling field 1:

$$\sigma_{Ed} = 110.1 \text{ N/mm}^2, \tau_{Ed} = 40.5 \text{ N/mm}^2$$

non-dimensional slenderness ratio  $\lambda_p = \lambda_c = \lambda_w = (\alpha_{ult}/\alpha_{cr})^{1/2} = 0.943$ ,  $\alpha_{ult} = 1.801$ ,  $\alpha_{cr} = 2.024$  (4H-tool)

reduction factor  $\rho = (\lambda_p - 0.055 \cdot (3 + \psi)) / \lambda_p^2 = 0.813 \leq 1$  for  $\lambda_p > 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.673$ ,  $\psi = 1.000$

reduction factor  $\chi_w = 0.83 / \lambda_w = 0.880$  for  $0.83 / \eta = 0.692 \leq \lambda_w < 1.08$

ultimate buckling stresses  $\sigma_{Rd} = \rho \cdot f_y / \gamma M_1 = 173.7 \text{ N/mm}^2$ ,  $\tau_{Rd} = \chi_w \cdot f_y / (3^{1/2} \cdot \gamma M_1) = 108.5 \text{ N/mm}^2$

verification:  $((\sigma_{Ed}/\sigma_{Rd})^2 + (\tau_{Ed}/\tau_{Rd})^2)^{1/2} = 0.735 < 1$  ok.

#### single buckling field 2:

$$\sigma_{Ed} = 110.1 \text{ N/mm}^2, \tau_{Ed} = 40.5 \text{ N/mm}^2$$

non-dimensional slenderness ratio  $\lambda_p = \lambda_c = \lambda_w = (\alpha_{ult}/\alpha_{cr})^{1/2} = 0.943$ ,  $\alpha_{ult} = 1.801$ ,  $\alpha_{cr} = 2.024$  (4H-tool)

reduction factor  $\rho = (\lambda_p - 0.055 \cdot (3 + \psi)) / \lambda_p^2 = 0.813 \leq 1$  for  $\lambda_p > 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.673$ ,  $\psi = 1.000$

reduction factor  $\chi_w = 0.83 / \lambda_w = 0.880$  for  $0.83 / \eta = 0.692 \leq \lambda_w < 1.08$

ultimate buckling stresses  $\sigma_{Rd} = \rho \cdot f_y / \gamma M_1 = 173.7 \text{ N/mm}^2$ ,  $\tau_{Rd} = \chi_w \cdot f_y / (3^{1/2} \cdot \gamma M_1) = 108.5 \text{ N/mm}^2$

verification:  $((\sigma_{Ed}/\sigma_{Rd})^2 + (\tau_{Ed}/\tau_{Rd})^2)^{1/2} = 0.735 < 1$  ok.

#### single buckling field 3:

$$\sigma_{Ed} = 110.1 \text{ N/mm}^2, \tau_{Ed} = 40.5 \text{ N/mm}^2$$

non-dimensional slenderness ratio  $\lambda_p = \lambda_c = \lambda_w = (\alpha_{ult}/\alpha_{cr})^{1/2} = 0.943$ ,  $\alpha_{ult} = 1.801$ ,  $\alpha_{cr} = 2.024$  (4H-tool)

reduction factor  $\rho = (\lambda_p - 0.055 \cdot (3 + \psi)) / \lambda_p^2 = 0.813 \leq 1$  for  $\lambda_p > 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.673$ ,  $\psi = 1.000$

reduction factor  $\chi_w = 0.83 / \lambda_w = 0.880$  for  $0.83 / \eta = 0.692 \leq \lambda_w < 1.08$

ultimate buckling stresses  $\sigma_{Rd} = \rho \cdot f_y / \gamma M_1 = 173.7 \text{ N/mm}^2$ ,  $\tau_{Rd} = \chi_w \cdot f_y / (3^{1/2} \cdot \gamma M_1) = 108.5 \text{ N/mm}^2$

verification:  $((\sigma_{Ed}/\sigma_{Rd})^2 + (\tau_{Ed}/\tau_{Rd})^2)^{1/2} = 0.735 < 1$  ok.

### overall buckling field:

$$\sigma_{Ed} = 110.1 \text{ N/mm}^2, \tau_{Ed} = 40.5 \text{ N/mm}^2$$

non-dimensional slenderness ratio  $\lambda_p = \lambda_c = \lambda_w = (\alpha_{ult}/\alpha_{cr})^{1/2} = 0.961$ ,  $\alpha_{ult} = 1.801$ ,  $\alpha_{cr} = 1.948$  (4H-tool)

reduction factor  $\rho = (\lambda_p - 0.055 \cdot (3 + \psi)) / \lambda_p^2 = 0.802 \leq 1$  for  $\lambda_p > 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.673$ ,  $\psi = 1.000$

critical buckling stress  $\sigma_{cr,p} = \alpha_{cr} \cdot \sigma_{Ed}' = 214.5 \text{ N/mm}^2$ ,  $\sigma_{Ed}' = 110.1 \text{ N/mm}^2$

critical buckling stress  $\sigma_{cr,c} = \sigma_{cr,c,sl} \cdot \sigma_1 / \sigma_{sl} = 177.8 \text{ N/mm}^2$ ,  $\sigma_1 / \sigma_{sl} = 1.000$ ,  $\sigma_{cr,c,sl} = 177.8 \text{ N/mm}^2$

reduction factor  $\chi_c = 0.514 \leq 1$  for  $\lambda_c > 0.2$

final reduction factor  $\rho = (\rho - \chi_c) \cdot \xi \cdot (2 - \xi) + \chi_c = 0.621$  with  $\xi = 0.206$

reduction factor  $\chi_w = 0.83 / \lambda_w = 0.863$  for  $0.83 / \eta = 0.692 \leq \lambda_w < 1.08$

ultimate buckling stresses  $\sigma_{Rd} = \rho \cdot f_y / \gamma M_1 = 132.6 \text{ N/mm}^2$ ,  $\tau_{Rd} = \chi_w \cdot f_y / (3^{1/2} \cdot \gamma M_1) = 106.5 \text{ N/mm}^2$

verification:  $((\sigma_{Ed}/\sigma_{Rd})^2 + (\tau_{Ed}/\tau_{Rd})^2)^{1/2} = 0.913 < 1$  ok.

longitudinal stiffeners: torsional buckling of stiffener  $I_{T,st} / I_{p,st} = 0.47\% < 5.3 \cdot f_y / E = 0.59\%$  ok.

transverse stiffeners:

rigid support of buckling field:

assumption: transverse stiffeners without axial force.

$I_{st} = 2510.06 \text{ cm}^4 > \sigma_m / E \cdot (b/\pi)^4 \cdot (1 + w_0 \cdot 300 \cdot u/b) = 10.60 \text{ cm}^4$  ok.

torsional buckling:

$I_{T,st} / I_{p,st} = 0.10\% < 5.3 \cdot f_y / E = 0.59\%$  ok.

minimum moment of inertia to ensure a rigid support:

$I_{sl} = 7105.27 \text{ cm}^4 > 0.75 \cdot h_w \cdot t^3 = 127.35 \text{ cm}^4$  ok. for  $a/h_w = 2.03 \geq 2^{1/2}$

total utilization:  $U = 0.913 < 1$  ok.

## Final Result

maximum utilization:

max  $U = 0.913 < 1$  ok.

assumptions:

succeeded ok.

verifications succeeded



## **Regulations**

DIN EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;  
Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010  
DIN EN 1990/NA, Nationaler Anhang zur DIN EN 1990, Ausgabe Dezember 2010

DIN EN 1993-1-1, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -  
Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;  
Deutsche Fassung EN 1993-1-1:2005 + AC:2009, Ausgabe Dezember 2010  
DIN EN 1993-1-1/NA, Nationaler Anhang zur DIN EN 1993-1-1, Ausgabe Dezember 2010

DIN EN 1993-1-5, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -  
Teil 1-5: Plattenförmige Bauteile;  
Deutsche Fassung EN 1993-1-5:2006 + AC:2009, Ausgabe Dezember 2010  
DIN EN 1993-1-5/NA, Nationaler Anhang zur DIN EN 1993-1-5, Ausgabe Dezember 2010

