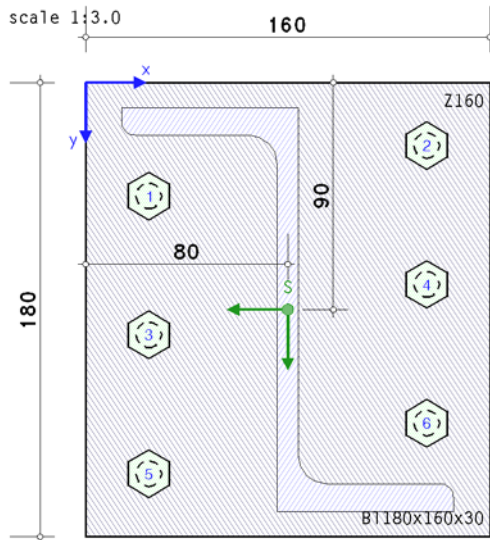


bolted end-plate connection

EC 3-1-8 (12.10), NA: Deutschland



steel grade

steel grade S355

bolts

bolt class 8.8, bolt size M10, thread included in the shear plane

connection

end-plate: thickness $t_p = 30.0$ mm, width $b_p = 160.0$ mm, length $l_p = 180.0$ mm

beam: section Z160

beam-end-plate: surrounding fillet weld, weld thickness $a = 10.0$ mm

beam section centric on end-plate (coinciding centroids)

coordinates of beam centroid on end-plate $x_s = 80.0$ mm, $y_s = 90.0$ mm

bolts:

coordinates of bolt axis:

$x_1 = 25.0$ mm, $y_1 = 45.0$ mm

$x_2 = 135.0$ mm, $y_2 = 25.0$ mm

$x_3 = 25.0$ mm, $y_3 = 100.0$ mm

$x_4 = 135.0$ mm, $y_4 = 80.0$ mm

$x_5 = 25.0$ mm, $y_5 = 155.0$ mm

$x_6 = 135.0$ mm, $y_6 = 135.0$ mm

calculation

verification:

calculation and verification of internal forces and moments (FEM)

verification of end-plate with the plastic method

verification of beam section with the plastic method

verification of welds with the directional method

verification of bolts, check of distances

FEM-calculation:

bolts are plastically calculated, spring constant of bolts $c_f = 2357.9$ kN/cm

plastic limit force $F_{t,f} = f_{t,f} \cdot F_{t,Rd} = 31.7$ kN, $f_{t,f} = 0.950$, $F_{t,Rd} = 33.4$ kN, effective elongation at failure $\epsilon_{t,f} = 6.0\%$

without preloading ($F_{p,c} = 0$)

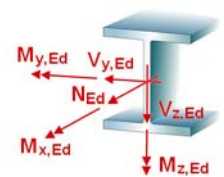
effective foundation modulus of end plate $c_b = 14000.0$ kN/cm³

number / dimension of finite elements each direction $n_x / \Delta x = 20 / 8.0$ mm, $n_y / \Delta y = 21 / 8.6$ mm

max. 50 iteration steps (tolerance limit 5‰)

internal forces and moments

Lk	N_{Ed} kN	$M_{y,Ed}$ kNm	$V_{z,Ed}$ kN	$M_{z,Ed}$ kNm	$V_{y,Ed}$ kN	$M_{x,Ed}$ kNm
1	-9.6	-0.5	0.8	2.6	1.4	0.8
2	8.4	3.0	23.1	10.4	5.1	0.0
3	-3.7	0.0	0.6	-5.6	-2.9	0.8
4	3.0	2.8	23.2	12.1	6.0	0.0
5	-8.9	-0.0	0.7	3.3	1.7	0.0
6	5.4	2.4	23.2	6.2	3.0	1.2
7	-2.9	0.5	0.5	-4.9	-2.6	-0.0
8	1.9	2.1	23.3	11.1	5.5	1.2
9	-3.9	1.3	16.6	9.6	4.8	0.8
10	-3.2	1.8	16.5	10.3	5.1	0.0



partial safety factors for material

resistance of cross-sections $\gamma_{M0} = 1.00$

Calculation

utilizations

Lk	U_p	U_σ	U_b	U_{wt}	$U_{t,s}$	$U_{vt,s}$	$U_{b,s}$	U_q	U_{ct}	U_w	U
1	0.065	0.065	0.054	0.015	0.196	0.227	0.010	0.354	0.204	0.204	0.354
2	0.295	0.295	0.245	0.129	0.950	0.709	0.034	0.419	0.479	0.748	0.950*
3	0.142	0.142	0.115	0.041	0.524	0.432	0.011	0.406	0.292	0.420	0.524
4	0.358	0.358	0.292	0.166	0.950	0.741	0.043	0.506	0.476	0.875	0.950*
5	0.086	0.086	0.070	0.022	0.275	0.208	0.002	0.160	0.226	0.250	0.275
6	0.161	0.161	0.142	0.061	0.780	0.586	0.030	0.541	0.487	0.441	0.780
7	0.122	0.122	0.096	0.035	0.445	0.332	0.002	0.254	0.275	0.373	0.445
8	0.320	0.320	0.248	0.117	0.950	0.690	0.033	0.666	0.473	0.808	0.950*
9	0.262	0.262	0.205	0.078	0.932	0.674	0.023	0.535	0.471	0.701	0.932
10	0.287	0.287	0.224	0.093	0.950	0.697	0.024	0.443	0.474	0.747	0.950*

U_p : utilization of end-plate; U_σ : utilization of end-plate due to stress; U_b : utilization of end-plate due to compression by contact
 $U_{wt,s}$: utilization of bolts due to elongation; $U_{t,s}$: utilization of bolts due to tension; $U_{vt,s}$: utilization of bolts due to shear in tension
 $U_{b,s}$: utilization of bolts due to bearing resistance; U_q : stress utilization of beam; U_{ct} : c/t-utilization of beam
 U_w : utilization of welds; U: total utilization
 *) maximum utilization

Final Result

maximum utilization [Lk 2] max U = 0.950 < 1 ok.

verification succeeded

Regulations

DIN EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;
 Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010
 DIN EN 1990/NA, Nationaler Anhang zur DIN EN 1990, Ausgabe Dezember 2010

DIN EN 1993-1-1, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -
 Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;
 Deutsche Fassung EN 1993-1-1:2005 + AC:2009, Ausgabe Dezember 2010
 DIN EN 1993-1-1/NA, Nationaler Anhang zur DIN EN 1993-1-1, Ausgabe Dezember 2010

DIN EN 1993-1-8, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -
 Teil 1-8: Bemessung von Anschlüssen;
 Deutsche Fassung EN 1993-1-8:2005 + AC:2009, Ausgabe Dezember 2010
 DIN EN 1993-1-8/NA, Nationaler Anhang zur DIN EN 1993-1-8, Ausgabe Dezember 2010

Detailed edition of Lk 2 (decisive)

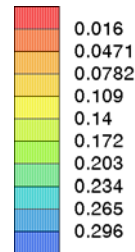
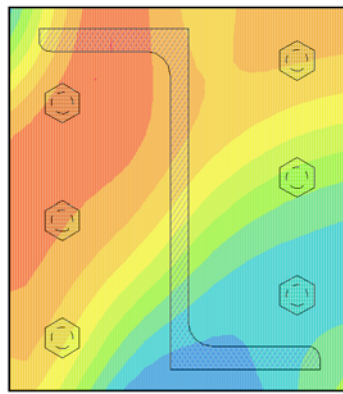
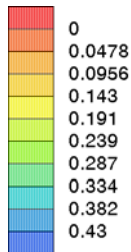
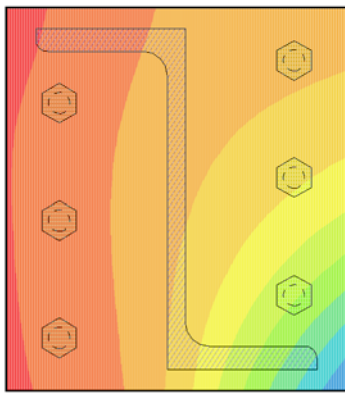
Lk 2: $N_{Ed} = 8.4 \text{ kN}$, $M_{y,Ed} = 3.0 \text{ kNm}$, $V_{z,Ed} = 23.1 \text{ kN}$, $M_{z,Ed} = 10.4 \text{ kNm}$, $V_{y,Ed}$

end-plate

design values: $N = 8.45 \text{ kN}$, $M_y = 2.97 \text{ kNm}$, $M_z = 10.43 \text{ kNm}$

deformations u_z [mm], lifting off positive
min $u_z = -0.02$ mm, max $u_z = 0.43$ mm

utilization of end-plate U_p
min $U_p = 0.016$, max $U_p = 0.295$



utilization of end-plate

Kno	x mm	y mm	u_z mm	U_σ	U_b	U_p
220	72.0	180.0	0.087	0.295	---	0.295
462	160.0	180.0	0.426	0.192	---	0.192

x,y: node coordinates; u_z : deformations (lifting off positive); U_σ : utilization due to moment with shear force; U_b : utilization due to compression by contact
 U_p : utilization of end-plate

tension force of bolts

	x mm	y mm	wt mm	F_t kN	ϵ_{wt} %	U_{wt}
1	25.0	45.0	0.017	3.89	0.055	0.009
2	135.0	25.0	0.085	20.04	0.283	0.047
3	25.0	100.0	0.021	4.94	0.070	0.012
4	135.0	80.0	0.135	30.84	0.449	0.075
5	25.0	155.0	0.014	3.38	0.048	0.008
6	135.0	135.0	0.232	31.74	0.774	0.129

x,y: bolt coordinates; wt: deformation (tension positive); F_t : bolt force; ϵ_{wt} : elongation
 U_{wt} : utilization due to elongation

utilization of end-plate [node 220] $U_{max} = 0.295 < 1$ ok.

utilization of bolts due to elongation [bolt 6] $U_{max} = 0.129 < 1$ ok.

bolts

design values: max $F_t = 31.74$ kN, $V_z = 23.13$ kN, $V_y = 5.10$ kN, $M_x = 0.05$ kNm

verification of bolts

U_{tp} utilization due to tension/punching shear failure, U_{vt} utilization due to shear in tension, U_b utilization due to bearing resistance, U utilization of bolts

bolt 1	$U_{tp,1} = 0.117$	$U_{vt,1} = 0.333$	$U_{b,1} = 0.019$	$U_1 = 0.333$
bolt 2	$U_{tp,2} = 0.600$	$U_{vt,2} = 0.667$	$U_{b,2} = 0.024$	$U_2 = 0.667$
bolt 3	$U_{tp,3} = 0.148$	$U_{vt,3} = 0.356$	$U_{b,3} = 0.020$	$U_3 = 0.356$
bolt 4	$U_{tp,4} = 0.923$	$U_{vt,4} = 0.704$	$U_{b,4} = 0.003$	$U_4 = 0.923$
bolt 5	$U_{tp,5} = 0.101$	$U_{vt,5} = 0.409$	$U_{b,5} = 0.034$	$U_5 = 0.409$
bolt 6	$U_{tp,6} = 0.950$	$U_{vt,6} = 0.709$	$U_{b,6} = 0.002$	$U_6 = 0.950$
total Max:	$U_{tp} = 0.950$	$U_{vt} = 0.709$	$U_b = 0.034$	$U = 0.950 < 1$ ok.

utilization of bolts [bolt 6] $U_{max} = 0.950 < 1$ ok.

beam

plastic cross-sectional check for $N = 8.45$ kN, $M_y = 6.31$ kNm, $V_z = 20.07$ kN,

$M_z = 8.82$ kNm, $V_y = 12.58$ kN, $M_x = 0.05$ kNm

valid normal-/shear stress: zul $\sigma_{Rd} = 35.50$ kN/cm², zul $\tau_{Rd} = 20.50$ kN/cm²

top flange: shear force $V_O = 2.55$ kN, torsion $T_{pO} = 0.02$ kNm, shear stress $\tau_O = 0.59$ kN/cm² $\Rightarrow U_{\tau,O} = 0.029$

flange bending $M_{\sigma,O} = 5.06$ kNm, bending stress $\sigma_O = 8.72$ kN/cm² $\Rightarrow U_{\sigma,O} = 0.246$

design resistance forces $N_{max,O} = -4.41$ kN, $N_{min,O} = -136.06$ kN

bottom flange: shear force $V_U = 2.55$ kN, torsion $T_{pU} = 0.02$ kNm, shear stress $\tau_U = 0.59$ kN/cm² $\Rightarrow U_{\tau,U} = 0.029$

flange bending $M_{\sigma,U} = 5.37$ kNm, bending stress $\sigma_U = 9.25$ kN/cm² $\Rightarrow U_{\sigma,U} = 0.261$

design resistance forces $N_{max,U} = 139.81$ kN, $N_{min,U} = 9.27$ kN

web: shear force $V_S = 23.13$ kN, torsion $T_{pS} = 0.01$ kNm, shear stress $\tau_S = 2.12$ kN/cm² $\Rightarrow U_{\tau,S} = 0.104$

design resistance forces $N_{max,S} = 414.17$ kN, $N_{min,S} = -414.17$ kN

main bending: axial force $N = 8.45$ kN, design resistance forces $N_{max} = 549.58$ kN, $N_{min} = -540.96$ kN $\Rightarrow U_N = 0.015$

moment $M_y = 2.97$ kNm, design resistance moments $M_{y,max} = 34.84$ kNm, $M_{y,min} = -13.27$ kNm $\Rightarrow U_{M_y} = 0.085$

total (possibly due to load increase): max $U = 0.419 < 1$ ok.

utilizations: design resistance $U_{\sigma} = 0.419 < 1$ **ok.**, c/t-ratio $U_{c/t} = 0.479 < 1$ **ok.**

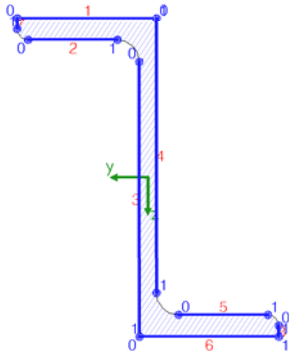
utilization of beam $\max(U_{\sigma}, U_{c/t}) = 0.479 < 1$ **ok.**

welds

design values: $N = 8.45$ kN, $M_y = 2.97$ kNm, $V_z = 23.13$ kN, $M_z = 10.43$ kNm,
 $V_y = 5.10$ kN, $M_x = 0.05$ kNm

weld 3: weld thickness $a = 10.0$ mm $> a_{\max} = t_{\min} = 6.0$ mm **!!**

weld 4: weld thickness $a = 10.0$ mm $> a_{\max} = t_{\min} = 6.0$ mm **!!**



weld 1:	$a_w = 10.0$ mm	$l_w = 70.0$ mm
weld 2:	$a_w = 10.0$ mm	$l_w = 45.0$ mm
weld 3:	$a_w = 10.0$ mm	$l_w = 138.0$ mm
weld 4:	$a_w = 10.0$ mm	$l_w = 138.0$ mm
weld 5:	$a_w = 10.0$ mm	$l_w = 45.0$ mm
weld 6:	$a_w = 10.0$ mm	$l_w = 70.0$ mm
weld 7:	$a_w = 10.0$ mm	$l_w = 5.5$ mm
weld 8:	$a_w = 10.0$ mm	$l_w = 5.5$ mm

Max: $\sigma_{1,w,Ed} = 32.57$ kN/cm² $< f_{1,w,Rd} = 43.56$ kN/cm²,
 $\sigma_{2,w,Ed} = 16.29$ kN/cm² $< f_{2,w,Rd} = 35.28$ kN/cm² $\Rightarrow U_w = 0.748 < 1$ **ok.**

utilization of welds $U_{\max} = 0.748 < 1$ **ok.**

utilization Lk 2 $U_{\max} = 0.950 < 1$ **ok.**