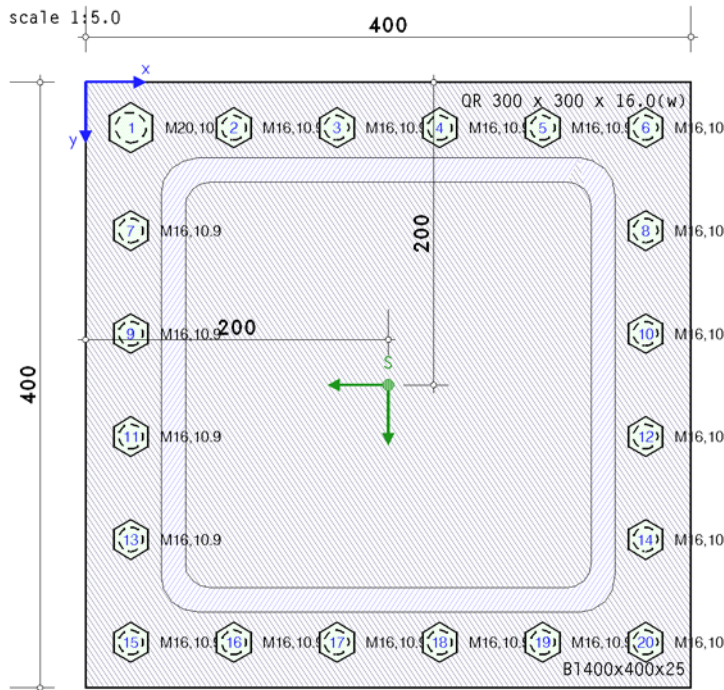


bolted end-plate connection

EC 3-1-8 (12.10), NA: Deutschland



steel grade

steel grade S235

bolts

thread included in the shear plane

--	FK	f_{yb} N/mm ²	f_{ub} N/mm ²	ϵ_{ub} %	TP	Schlüss	d mm	Δd mm	A mm ²	A_s mm ²	d_{ks} mm	d_{ke} mm	t_k mm	t_m mm	d_p mm	t_p mm
1	10.9	900.0	1000.0	9.0	M20	normal	20.0	2.0	314.2	245.0	30.0	33.0	12.5	19.0	37.0	3.0
2	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
3	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
4	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
5	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
6	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
7	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
8	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
9	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
10	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
11	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
12	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
13	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
14	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
15	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
16	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
17	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
18	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
19	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0
20	10.9	900.0	1000.0	9.0	M16	normal	16.0	2.0	201.1	157.0	24.0	26.2	10.0	15.9	30.0	3.0

FK: bolt class; f_{yb} : char. yield strength; f_{ub} : char. tensile strength; ϵ_{ub} : elongation at failure

TP: bolt size; Schlüss: cross flats dimension; d: nominal value of bolt diameter; Δd : clearance

A: gross section (shaft); A_s : cross-section under stress; d_{ks} : across flats dimension of bolt head; d_{ke} : across points dimension of bolt head

t_k : thickness of the bolt head; t_m : nut height; d_p : diameter of a washer; t_p : plate thickness of a washer

connection

end-plate: thickness $t_p = 25.0$ mm, width $b_p = 400.0$ mm, length $l_p = 400.0$ mm

beam: section QR 300 x 300 x 16.0(w)

beam-end-plate: surrounding butt weld (full penetrated)

beam section centric on end-plate (coinciding centroids)

coordinates of beam centroid on end-plate $x_s = 200.0$ mm, $y_s = 200.0$ mm

bolts:

	x mm	y mm	FK	TP	Schlüss	c_f kN/cm	$f_{t,f}$	$F_{t,Rd}$ kN	$F_{t,f}$ kN	$\epsilon_{t,f}$ %	$F_{p,C}$ kN
1	30.0	30.0	10.9	M20	normal	9596.1	0.950	176.4	167.6	4.5	--
2	98.0	30.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
3	166.0	30.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
4	234.0	30.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
5	302.0	30.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
6	370.0	30.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
7	30.0	98.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--

	x mm	y mm	FK	TP	Schlüss	c _f kN/cm	f _{t,f}	F _{t,Rd} kN	F _{t,f} kN	ε _{t,f} %	F _{p,C} kN
8	370.0	98.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
9	30.0	166.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
10	370.0	166.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
11	30.0	234.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
12	370.0	234.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
13	30.0	302.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
14	370.0	302.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
15	30.0	370.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
16	98.0	370.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
17	166.0	370.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
18	234.0	370.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
19	302.0	370.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--
20	370.0	370.0	10.9	M16	normal	6402.3	0.950	113.0	107.4	4.5	--

x,y: coordinates of bolt axis on end-plate; FK: bolt class; TP: bolt size

Schlüss: across flats dimension; c_f: spring stiffness of bolt (FEM); f_{t,f}: usage factor of spring (FEM)

F_{t,Rd}: max. tension force of bolt (FEM); F_{t,f} = f_{t,f}·F_{t,Rd}: plastic limit force of bolt (FEM); ε_{t,f}: elongation at failure of bolt (FEM)

F_{p,C}: preload force of bolt (FEM); F_{p,C}: preload force of bolt (FEM)

calculation

verification:

calculation and verification of internal forces and moments (FEM)

verification of end-plate with the plastic method

verification of beam section with the elastic method

verification of welds with the directional method

verification of bolts, check of distances

FEM-calculation:

bolts are plasticly calculated (c_f, F_{t,Rd}, F_{t,f}, f_{t,f}, ε_{t,f}, F_{p,C} s. table)

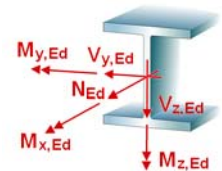
effective foundation modulus of end plate c_b = 16800.0 kN/cm³

number / dimension of finite elements each direction n_x / Δx = 25 / 16.0 mm, n_y / Δy = 25 / 16.0 mm

max. 50 iteration steps (tolerance limit 5‰)

internal forces and moments

Lk	N _{Ed} kN	M _{y,Ed} kNm	V _{z,Ed} kN	M _{z,Ed} kNm	V _{y,Ed} kN	M _{x,Ed} kNm
1	-171.7	-199.4	-44.3	-130.9	29.1	10.6
2	33.3	6.5	1.5	103.0	-12.8	22.5
3	-160.3	-156.0	-34.7	-190.0	42.2	-13.5
4	-70.5	-30.1	-6.7	-169.5	37.7	-36.4
5	-109.3	-177.4	-39.4	32.6	-1.2	45.9



partial safety factors for material

resistance of cross-sections γ_{M0} = 1.00

resistance of bolts, welds, plates in bearing γ_{M2} = 1.25

Calculation

utilizations

Lk	U _p	U _σ	U _b	U _{w,t}	U _{t,s}	U _{v,t,s}	U _{b,s}	U _q	U _{c/t}	U _w	U
--	--	--	--	--	--	--	--	--	--	--	--
1	0.631	0.631	0.392	0.197	0.949	0.683	0.046	0.885	0.248	0.763	0.949*
2	0.218	0.218	0.123	0.072	0.459	0.410	0.076	0.307	0.175	0.256	0.459
3	0.659	0.659	0.417	0.249	0.950	0.685	0.060	0.922	0.241	0.792	0.950*
4	0.370	0.370	0.235	0.098	0.607	0.529	0.094	0.550	0.230	0.464	0.607
5	0.374	0.374	0.245	0.127	0.807	0.650	0.135	0.585	0.238	0.498	0.807

U_p: utilization of end-plate; U_σ: utilization of end-plate due to stress; U_b: utilization of end-plate due to compression by contact

U_{w,t,s}: utilization of bolts due to elongation; U_{t,s}: utilization of bolts due to tension; U_{v,t,s}: utilization of bolts due to shear in tension

U_{b,s}: utilization of bolts due to bearing resistance; U_q: stress utilization of beam; U_{c/t}: c/t-utilization of beam

U_w: utilization of welds; U: total utilization

*) maximum utilization

Final Result

maximum utilization [Lk 1] max U = 0.949 < 1 ok.

verification succeeded

Regulations

DIN EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;

Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010

DIN EN 1990/NA, Nationaler Anhang zur DIN EN 1990, Ausgabe Dezember 2010

DIN EN 1993-1-1, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;

Detailed edition of Lk 1 (decisive)

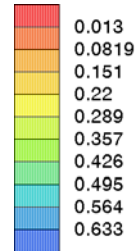
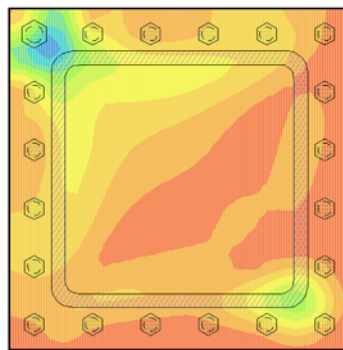
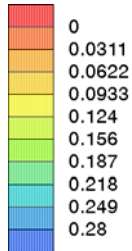
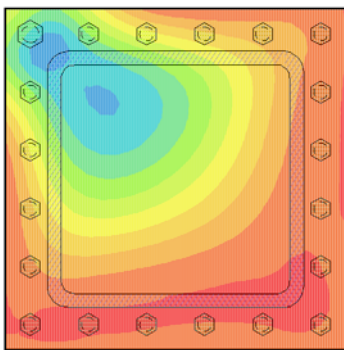
Lk 1: $N_{Ed} = -171.7 \text{ kN}$, $M_{y,Ed} = -199.4 \text{ kNm}$, $V_{z,Ed} = -44.3 \text{ kN}$, $M_{z,Ed} = -130.9 \text{ kNm}$,

end-plate

design values: $N = -171.66 \text{ kN}$, $M_y = -199.41 \text{ kNm}$, $M_z = -130.93 \text{ kNm}$

deformations u_z [mm], lifting off positive
 min $u_z = -0.01 \text{ mm}$, max $u_z = 0.28 \text{ mm}$

utilization of end-plate U_p
 min $U_p = 0.013$, max $U_p = 0.631$



utilization of end-plate

Kno	x mm	y mm	u_z mm	U_σ	U_b	U_p
82	48.0	48.0	0.278	0.631	---	0.631

x,y: node coordinates; u_z : deformations (lifting off positive); U_σ : utilization due to moment with shear force; U_b : utilization due to compression by contact
 U_p : utilization of end-plate

tension force of bolts

	x mm	y mm	w _t mm	F_t kN	ϵ_{wt} %	U_{wt}
1	30.0	30.0	0.222	167.46	0.888	0.197
2	98.0	30.0	0.187	105.21	0.746	0.166
3	166.0	30.0	0.104	66.67	0.417	0.093
4	234.0	30.0	0.066	42.43	0.265	0.059
5	302.0	30.0	0.046	29.60	0.185	0.041
6	370.0	30.0	0.018	11.66	0.073	0.016
7	30.0	98.0	0.182	103.91	0.726	0.161
8	370.0	98.0	0.012	7.46	0.047	0.010
9	30.0	166.0	0.097	61.79	0.386	0.086
10	370.0	166.0	0.006	3.87	0.024	0.005
11	30.0	234.0	0.055	35.13	0.219	0.049
12	370.0	234.0	0.002	1.53	0.010	0.002
13	30.0	302.0	0.025	15.71	0.098	0.022
14	370.0	302.0	-0.000	0.33	---	---
15	30.0	370.0	-0.001	0.12	---	---
16	98.0	370.0	-0.001	0.01	---	---
17	166.0	370.0	-0.001	0.15	---	---
18	234.0	370.0	0.000	0.61	0.002	---
19	302.0	370.0	-0.000	0.75	---	---
20	370.0	370.0	0.000	1.10	---	---

x,y: bolt coordinates; w_t : deformation (tension positive); F_t : bolt force; ϵ_{wt} : elongation
 U_{wt} : utilization due to elongation

utilization of end-plate [node 82] $U_{max} = 0.631 < 1$ ok.

utilization of bolts due to elongation [bolt 1] $U_{max} = 0.197 < 1$ ok.

bolts

design values: max $F_t = 167.46 \text{ kN}$, $V_z = -44.31 \text{ kN}$, $V_y = 29.10 \text{ kN}$, $M_x = 10.62 \text{ kNm}$

verification of bolts

U_{tp} utilization due to tension/punching shear failure, U_{vt} utilization due to shear in tension, U_b utilization due to bearing resistance, U utilization of bolts

bolt 1	$U_{tp,1} = 0.949$	$U_{vt,1} = 0.683$	$U_{b,1} = 0.004$	$U_1 = 0.949$
bolt 2	$U_{tp,2} = 0.931$	$U_{vt,2} = 0.672$	$U_{b,2} = 0.001$	$U_2 = 0.931$
bolt 3	$U_{tp,3} = 0.590$	$U_{vt,3} = 0.462$	$U_{b,3} = 0.010$	$U_3 = 0.590$
bolt 4	$U_{tp,4} = 0.375$	$U_{vt,4} = 0.336$	$U_{b,4} = 0.018$	$U_4 = 0.375$
bolt 5	$U_{tp,5} = 0.262$	$U_{vt,5} = 0.275$	$U_{b,5} = 0.025$	$U_5 = 0.275$
bolt 6	$U_{tp,6} = 0.103$	$U_{vt,6} = 0.192$	$U_{b,6} = 0.046$	$U_6 = 0.192$
bolt 7	$U_{tp,7} = 0.919$	$U_{vt,7} = 0.663$	$U_{b,7} = 0.002$	$U_7 = 0.919$
bolt 8	$U_{tp,8} = 0.066$	$U_{vt,8} = 0.157$	$U_{b,8} = 0.033$	$U_8 = 0.157$
bolt 9	$U_{tp,9} = 0.547$	$U_{vt,9} = 0.416$	$U_{b,9} = 0.010$	$U_9 = 0.547$
bolt 10	$U_{tp,10} = 0.034$	$U_{vt,10} = 0.126$	$U_{b,10} = 0.028$	$U_{10} = 0.126$
bolt 11	$U_{tp,11} = 0.311$	$U_{vt,11} = 0.248$	$U_{b,11} = 0.010$	$U_{11} = 0.311$
bolt 12	$U_{tp,12} = 0.014$	$U_{vt,12} = 0.104$	$U_{b,12} = 0.023$	$U_{12} = 0.104$
bolt 13	$U_{tp,13} = 0.139$	$U_{vt,13} = 0.117$	$U_{b,13} = 0.005$	$U_{13} = 0.139$
bolt 14	$U_{tp,14} = 0.003$	$U_{vt,14} = 0.092$	$U_{b,14} = 0.020$	$U_{14} = 0.092$
bolt 15	$U_{tp,15} = 0.001$	$U_{vt,15} = 0.018$	$U_{b,15} = 0.007$	$U_{15} = 0.018$
bolt 16	$U_{tp,16} = 0.000$	$U_{vt,16} = 0.000$	$U_{b,16} = 0.003$	$U_{16} = 0.010$
bolt 17	$U_{tp,17} = 0.001$	$U_{vt,17} = 0.029$	$U_{b,17} = 0.011$	$U_{17} = 0.029$
bolt 18	$U_{tp,18} = 0.005$	$U_{vt,18} = 0.052$	$U_{b,18} = 0.019$	$U_{18} = 0.052$
bolt 19	$U_{tp,19} = 0.007$	$U_{vt,19} = 0.073$	$U_{b,19} = 0.027$	$U_{19} = 0.073$
bolt 20	$U_{tp,20} = 0.010$	$U_{vt,20} = 0.096$	$U_{b,20} = 0.035$	$U_{20} = 0.096$
total Max:	$U_{tp} = 0.949$	$U_{vt} = 0.683$	$U_b = 0.046$	$U = 0.949 < 1$ ok.

utilization of bolts [bolt 1] $U_{max} = 0.949 < 1$ **ok.**

beam

elastic cross-sectional check for $N = -171.66$ kN, $M_y = -199.41$ kNm, $V_z = -44.31$ kN, $M_z = -130.93$ kNm, $V_y = 29.10$ kN, $M_x = 10.62$ kNm

max σ_v bei $y = -143.0$ mm, $z = 143.0$ mm: $\sigma_x = -20.76$ kN/cm², $\tau = 0.58$ kN/cm², $\sigma_v = 20.79$ kN/cm²

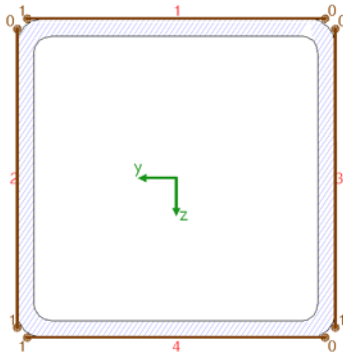
verification: $\sigma_v = 20.79$ kN/cm² < zul $\sigma_v = 23.50$ kN/cm² $\Rightarrow U = 0.885 < 1$ **ok.**

utilizations: design resistance $U_\sigma = 0.885 < 1$ **ok.**, c/t-ratio $U_{c/t} = 0.248 < 1$ **ok.**

utilization of beam $\max(U_\sigma, U_{c/t}) = 0.885 < 1$ **ok.**

welds

design values: $N = -171.66$ kN, $M_y = -199.41$ kNm, $V_z = -44.31$ kN, $M_z = -130.93$ kNm, $V_y = 29.10$ kN, $M_x = 10.62$ kNm



weld 1:	$a_w = 16.0$ mm	$l_w = 281.2$ mm
weld 2:	$a_w = 16.0$ mm	$l_w = 281.2$ mm
weld 3:	$a_w = 16.0$ mm	$l_w = 281.2$ mm
weld 4:	$a_w = 16.0$ mm	$l_w = 281.2$ mm

Max: $\sigma_{1,w,Ed} = 27.46$ kN/cm² < $f_{1,w,Rd} = 36.00$ kN/cm²,

$\sigma_{2,w,Ed} = 13.73$ kN/cm² < $f_{2,w,Rd} = 25.92$ kN/cm² $\Rightarrow U_w = 0.763 < 1$ **ok.**

utilization of welds $U_{max} = 0.763 < 1$ **ok.**

utilization Lk 1 $U_{max} = 0.949 < 1$ **ok.**