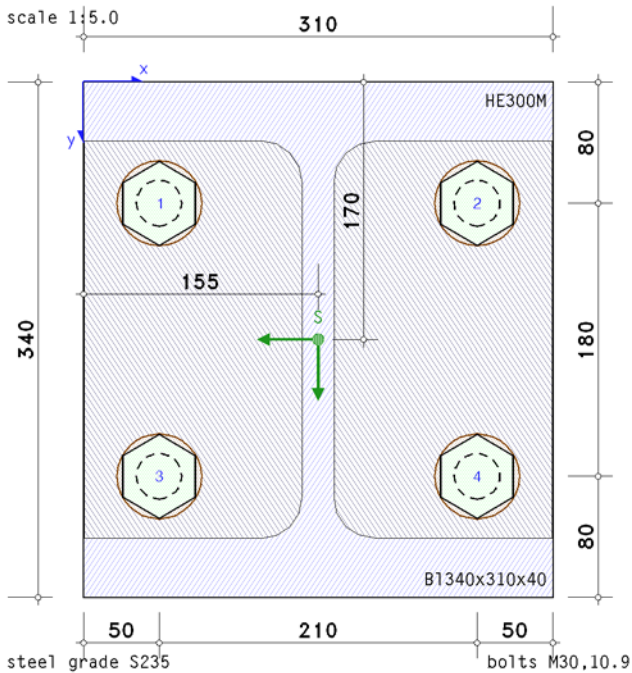


**bolted end-plate connection**

EC 3-1-8 (12.10), NA: Deutschland



**steel grade**

steel grade S235

**bolts**

bolts with big width across flats have to be preloaded with  $F_{p,c}$  !!

bolt class 10.9, bolt size M30

large width across flats (high strength bolt), controlled preloading  $F_{p,c}^* = 0.7 \cdot f_y \cdot A_s = 353.4$  kN, thread included in the shear plane

**connection**

end-plate: thickness  $t_p = 40.0$  mm, width  $b_p = 310.0$  mm, length  $l_p = 340.0$  mm

beam: section HE300M

beam-end-plate: surrounding fillet weld, weld thickness  $a = 8.0$  mm

beam section centric on end-plate (coinciding centroids)

coordinates of beam centroid on end-plate  $x_s = 155.0$  mm,  $y_s = 170.0$  mm

bolts:

uniform arrangement of bolts, 2 vertical and 2 horizontal rows

edge distances top, bottom  $e_o = e_u = 80.0$  mm, distances between bolts  $p_x = 210.0$  mm

edge distances left, right  $e_l = e_r = 50.0$  mm, distances between bolts  $p_y = 180.0$  mm

**calculation**

verification:

calculation and verification of internal forces and moments (FEM)

verification of end-plate with the plastic method

verification of beam section with the plastic method

verification of welds with the directional method

verification of bolts, check of distances

FEM-calculation:

bolts are plastically calculated, spring constant of bolts  $c_f = 13331.0$  kN/cm

plastic limit force  $F_{t,f} = f_{t,f} \cdot F_{t,Rd} = 383.7$  kN,  $f_{t,f} = 0.950$ ,  $F_{t,Rd} = 403.9$  kN, effective elongation at failure  $\epsilon_{t,f} = 4.5\%$

preload force  $F_{p,c} = 353.4$  kN

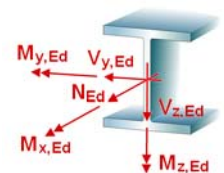
effective foundation modulus of end plate  $c_b = 10500.0$  kN/cm<sup>3</sup>

number / dimension of finite elements each direction  $n_x / \Delta x = 20 / 15.5$  mm,  $n_y / \Delta y = 20 / 17.0$  mm

max. 50 iteration steps (tolerance limit 5‰)

**internal forces and moments**

Lk	$N_{Ed}$ kN	$M_{y,Ed}$ kNm	$V_{z,Ed}$ kN	$M_{z,Ed}$ kNm	$V_{y,Ed}$ kN	$M_{x,Ed}$ kNm
1	-190.6	227.5	45.5	57.3	-11.5	0.1
2	21.5	28.0	5.6	-66.9	-5.4	-0.1
3	-98.5	100.9	20.2	67.5	-13.5	0.1
4	-75.4	88.7	17.7	0.8	-0.2	0.0
5	-24.7	-1.4	-0.3	47.1	-9.4	0.0
6	-162.9	245.2	49.0	-11.1	-9.0	0.0



Lk	N <sub>Ed</sub> kN	M <sub>y,Ed</sub> kNm	V <sub>z,Ed</sub> kN	M <sub>z,Ed</sub> kNm	V <sub>y,Ed</sub> kN	M <sub>x,Ed</sub> kNm
7	-26.6	84.0	16.8	-67.2	-5.3	-0.1
8	-122.0	147.5	29.5	57.7	-11.5	0.1
9	-161.6	237.5	47.5	-13.0	-8.7	0.0
10	-25.6	3.9	0.8	48.4	-9.7	0.0

#### partial safety factors for material

resistance of cross-sections  $\gamma_{M0} = 1.00$

resistance of bolts, welds, plates in bearing  $\gamma_{M2} = 1.25$

## Calculation

parts of fillet weld outside of end plate !

#### utilizations

Lk	U <sub>p</sub>	U <sub>σ</sub>	U <sub>b</sub>	U <sub>wt</sub>	U <sub>t,s</sub>	U <sub>vt,s</sub>	U <sub>b,s</sub>	U <sub>q</sub>	U <sub>ct</sub>	U <sub>w</sub>	U
1	0.927	0.927	0.729	0.559	0.950	0.725	0.024	0.308	0.145	0.988	0.988*
2	0.310	0.226	0.310	0.054	0.890	0.644	0.004	0.153	0.101	0.455	0.890
3	0.394	0.394	0.325	0.072	0.936	0.685	0.012	0.199	0.123	0.677	0.936
4	0.167	0.139	0.167	0.053	0.878	0.647	0.006	0.096	0.072	0.265	0.878
5	0.222	0.102	0.222	0.053	0.876	0.636	0.005	0.107	0.081	0.274	0.876
6	0.699	0.644	0.699	0.378	0.950	0.727	0.023	0.272	0.124	0.770	0.950
7	0.370	0.370	0.305	0.069	0.929	0.677	0.008	0.183	0.117	0.608	0.929
8	0.526	0.526	0.365	0.112	0.950	0.697	0.016	0.227	0.128	0.754	0.950
9	0.630	0.630	0.606	0.317	0.950	0.721	0.023	0.266	0.123	0.759	0.950
10	0.228	0.109	0.228	0.053	0.876	0.637	0.006	0.110	0.083	0.288	0.876

U<sub>p</sub>: utilization of end-plate; U<sub>σ</sub>: utilization of end-plate due to stress; U<sub>p</sub>: utilization of end-plate due to compression by contact

U<sub>wt,s</sub>: utilization of bolts due to elongation; U<sub>t,s</sub>: utilization of bolts due to tension; U<sub>vt,s</sub>: utilization of bolts due to shear in tension

U<sub>b,s</sub>: utilization of bolts due to bearing resistance; U<sub>q</sub>: stress utilization of beam; U<sub>ct</sub>: c/t-utilization of beam

U<sub>w</sub>: utilization of welds; U: total utilization

\*) maximum utilization

## Final Result

maximum utilization [Lk 1] max U = 0.988 < 1 ok.

verification succeeded

## Regulations

DIN EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;

Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010

DIN EN 1990/NA, Nationaler Anhang zur DIN EN 1990, Ausgabe Dezember 2010

DIN EN 1993-1-1, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;

Deutsche Fassung EN 1993-1-1:2005 + AC:2009, Ausgabe Dezember 2010

DIN EN 1993-1-1/NA, Nationaler Anhang zur DIN EN 1993-1-1, Ausgabe Dezember 2010

DIN EN 1993-1-8, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-8: Bemessung von Anschlüssen;

Deutsche Fassung EN 1993-1-8:2005 + AC:2009, Ausgabe Dezember 2010

DIN EN 1993-1-8/NA, Nationaler Anhang zur DIN EN 1993-1-8, Ausgabe Dezember 2010

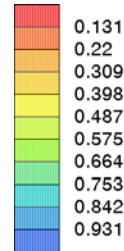
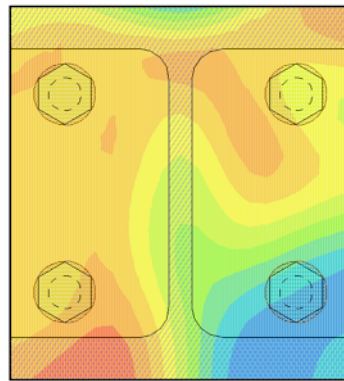
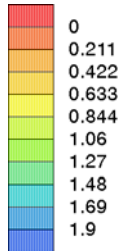
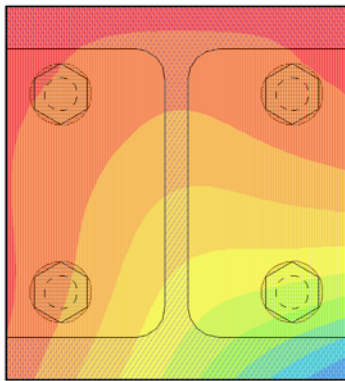
## Detailed edition of Lk 1 (decisive)

## end-plate

design values:  $N = -190.57 \text{ kN}$ ,  $M_y = 227.47 \text{ kNm}$ ,  $M_z = 57.30 \text{ kNm}$

deformations  $u_z$  [mm], lifting off positive  
min  $u_z = -0.05 \text{ mm}$ , max  $u_z = 1.93 \text{ mm}$

utilization of end-plate  $U_p$   
min  $U_p = 0.131$ , max  $U_p = 0.927$



## utilization of end-plate

Kno	x mm	y mm	$u_z$ mm	$U_\sigma$	$U_b$	$U_p$
336	232.5	340.0	1.438	0.927	---	0.927
441	310.0	340.0	1.929	0.757	---	0.757

x,y: node coordinates;  $u_z$ : deformations (lifting off positive);  $U_\sigma$ : utilization due to moment with shear force;  $U_b$ : utilization due to compression by contact  
 $U_p$ : utilization of end-plate

## tension force of bolts

	x mm	y mm	$w_t$ mm	$F_t$ kN	$\epsilon_{wt}$ %	$U_{wt}$
1	50.0	80.0	0.020	370.16	0.288	0.064
2	260.0	80.0	0.045	378.19	0.351	0.078
3	50.0	260.0	0.183	383.72	0.695	0.154
4	260.0	260.0	0.911	383.72	2.515	0.559

x,y: bolt coordinates;  $w_t$ : deformation (tension positive);  $F_t$ : bolt force;  $\epsilon_{wt}$ : elongation  
 $U_{wt}$ : utilization due to elongation

utilization of end-plate [node 336]  $U_{max} = 0.927 < 1$  **ok.**

utilization of bolts due to elongation [bolt 4]  $U_{max} = 0.559 < 1$  **ok.**

## bolts

design values: max  $F_t = 383.72 \text{ kN}$ ,  $V_z = 45.49 \text{ kN}$ ,  $V_y = -11.46 \text{ kN}$ ,  $M_x = 0.08 \text{ kNm}$

## verification of bolts

$U_{tp}$  utilization due to tension/punching shear failure,  $U_{vt}$  utilization due to shear in tension,  $U_b$  utilization due to bearing resistance,  $U$  utilization of bolts

bolt 1	$U_{tp,1} = 0.916$	$U_{vt,1} = 0.725$	$U_{b,1} = 0.024$	$U_1 = 0.916$
bolt 2	$U_{tp,2} = 0.936$	$U_{vt,2} = 0.723$	$U_{b,2} = 0.018$	$U_2 = 0.936$
bolt 3	$U_{tp,3} = 0.950$	$U_{vt,3} = 0.720$	$U_{b,3} = 0.014$	$U_3 = 0.950$
bolt 4	$U_{tp,4} = 0.950$	$U_{vt,4} = 0.721$	$U_{b,4} = 0.014$	$U_4 = 0.950$
total Max:	$U_{tp} = 0.950$	$U_{vt} = 0.725$	$U_b = 0.024$	$U = 0.950 < 1$ <b>ok.</b>

utilization of bolts [bolt 3]  $U_{max} = 0.950 < 1$  **ok.**

## beam

plastic cross-sectional check for  $N = -190.57 \text{ kN}$ ,  $M_y = 227.47 \text{ kNm}$ ,  $V_z = 45.49 \text{ kN}$ ,  
 $M_z = 57.30 \text{ kNm}$ ,  $V_y = -11.46 \text{ kN}$ ,  $M_x = 0.08 \text{ kNm}$

valid normal-/shear stress: zul  $\sigma_{Rd} = 23.50 \text{ kN/cm}^2$ , zul  $\tau_{Rd} = 13.57 \text{ kN/cm}^2$

top flange: shear force  $V_O = -5.73 \text{ kN}$ , torsion  $T_{pO} = 0.04 \text{ kNm}$ , shear stress  $\tau_O = 0.06 \text{ kN/cm}^2 \Rightarrow U_{\tau,O} = 0.004$   
flange bending  $M_{\sigma,O} = 28.65 \text{ kNm}$ , bending stress  $\sigma_O = 3.06 \text{ kN/cm}^2 \Rightarrow U_{\sigma,O} = 0.130$   
design resistance forces  $N_{max,O} = 2649.85 \text{ kN}$ ,  $N_{min,O} = -2649.85 \text{ kN}$

bottom flange: shear force  $V_U = -5.73 \text{ kN}$ , torsion  $T_{pU} = 0.04 \text{ kNm}$ , shear stress  $\tau_U = 0.06 \text{ kN/cm}^2 \Rightarrow U_{\tau,U} = 0.004$   
flange bending  $M_{\sigma,U} = 28.65 \text{ kNm}$ , bending stress  $\sigma_U = 3.06 \text{ kN/cm}^2 \Rightarrow U_{\sigma,U} = 0.130$   
design resistance forces  $N_{max,U} = 2649.85 \text{ kN}$ ,  $N_{min,U} = -2649.85 \text{ kN}$

web: shear force  $V_S = 45.49 \text{ kN}$ , torsion  $T_{pS} = 0.01 \text{ kNm}$ , shear stress  $\tau_S = 0.72 \text{ kN/cm}^2 \Rightarrow U_{\tau,S} = 0.053$   
design resistance forces  $N_{max,S} = 1483.32 \text{ kN}$ ,  $N_{min,S} = -1483.32 \text{ kN}$

main bending: axial force  $N = -190.57 \text{ kN}$ , design resistance forces  $N_{max} = 6783.02 \text{ kN}$ ,  $N_{min} = -6783.02 \text{ kN} \Rightarrow U_N = 0.028$   
moment  $M_y = 227.47 \text{ kNm}$ , design resistance moments  $M_{y,max} = 907.38 \text{ kNm}$ ,  $M_{y,min} = -907.38 \text{ kNm} \Rightarrow U_{M_y} = 0.25$

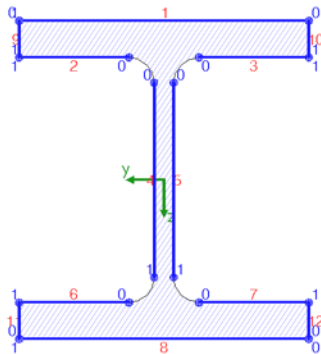
total (possibly due to load increase):  $\max U = 0.308 < 1$  **ok.**

utilizations: design resistance  $U_{\sigma} = 0.308 < 1$  **ok.**, c/t-ratio  $U_{c/t} = 0.145 < 1$  **ok.**

utilization of beam  $\max(U_{\sigma}, U_{c/t}) = 0.308 < 1$  **ok.**

## welds

design values:  $N = -190.57$  kN,  $M_y = 227.47$  kNm,  $V_z = 45.49$  kN,  $M_z = 57.30$  kNm,  
 $V_y = -11.46$  kN,  $M_x = 0.08$  kNm



weld 1:	$a_w = 8.0$ mm	$l_w = 310.0$ mm
weld 2:	$a_w = 8.0$ mm	$l_w = 117.5$ mm
weld 3:	$a_w = 8.0$ mm	$l_w = 117.5$ mm
weld 4:	$a_w = 8.0$ mm	$l_w = 208.0$ mm
weld 5:	$a_w = 8.0$ mm	$l_w = 208.0$ mm
weld 6:	$a_w = 8.0$ mm	$l_w = 117.5$ mm
weld 7:	$a_w = 8.0$ mm	$l_w = 117.5$ mm
weld 8:	$a_w = 8.0$ mm	$l_w = 310.0$ mm
weld 9:	$a_w = 8.0$ mm	$l_w = 39.0$ mm
weld 10:	$a_w = 8.0$ mm	$l_w = 39.0$ mm
weld 11:	$a_w = 8.0$ mm	$l_w = 39.0$ mm
weld 12:	$a_w = 8.0$ mm	$l_w = 39.0$ mm

Max:  $\sigma_{1,w,Ed} = 35.55$  kN/cm<sup>2</sup> <  $f_{1,w,Rd} = 36.00$  kN/cm<sup>2</sup>,

$\sigma_{2,w,Ed} = 17.78$  kN/cm<sup>2</sup> <  $f_{2,w,Rd} = 25.92$  kN/cm<sup>2</sup>  $\Rightarrow U_w = 0.988 < 1$  **ok.**

utilization of welds  $U_{\max} = 0.988 < 1$  **ok.**

utilization Lk 1  $U_{\max} = 0.988 < 1$  **ok.**